

Short Paper

Ranking Genes for Discriminability on Microarray Data

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This paper proposes a new feature selection method, called weighted pnishment on overlap (WEPO), for microarray data analysis. WEPO takes advantage of parametric and nonparametric estimations to rank genes sensitively despite the limited number of samples. The proposed method was implemented and applied to three datasets. Based on informative testing, sensitivity testing, and significance testing, we analyzed the performance of WEPO and five well-known feature selection methods. Analysis results indicate that genes selected using WEPO are more informative and sensitive than those selected using the other surveyed methods and are statistically significant. Biological results also show that WEPO is able to identify meaningful genes for test data sets. The analysis and experimental results indicate that WEPO is a promising approach to select important genes in a microarray data.

Keywords: feature selection, microarray, weighted punishment on overlap, z-score, support vector machine, ranking-based

1. INTRODUCTION

Microarrays have provided a way to measure the expression levels of a large number of genes simultaneously. Researchers have developed diagnostic tools by adapting this technique to profile the gene expression patterns of disease tissues [1-3]. Such profiling data may involve many thousands of genes and hundreds of tissue samples. The tissues are labeled according to certain classes, such as normal or tumor tissues. Genes that are differentially expressed in two classes are thought of as relevant genes. However, many genes in the profiling data may be irrelevant to the disease and result in incorrect clustering and misclassifications. To eliminate those “probable noise” genes, some feature selection approaches have been proposed to select informative and discriminative genes from the profiling data.

Feature selection methods, which have received much attention in the classification literature [4, 5], can be roughly divided into linear combination and ranking approaches

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in microarray data analysis. Linear combination approaches simplify the complex data by finding some new variables which are linear combinations of the original variables. For instance, principal component analysis (PCA) [6], an exploratory multivariate statistical technique, finds some mutually uncorrelated and orthogonal principal components to reduce the dimensionality of the data matrix. However, this kind of method cannot discover relevant genes individually.

Ranking methods, on the other hand, score the discriminability of each gene based only on its own expression patterns. Two major scoring metrics of discriminability, parametric and non parametric estimations, have been proposed for carrying out such analysis. Parametric estimation approaches assess the discriminability of genes by using different statistical criteria to estimate the degree of compactness within the same classes and the separation between two classes [3, 7, 8]. Parametric estimation approaches rank genes apart apparently. However, many statistical criteria are based on the assumption that the data come from some kind of distribution. With thousands of genes and only a small number of samples, the information may be lost since it is reduced to just a few estimators, such as values of mean and standard deviation. Thus, the process of detecting irrelevant genes can suffer from statistical instability [9].

Nonparametric estimation approaches sort samples according to the expression levels a gene produces and make punishments on the disorder of ambiguous samples which damage a perfect split of different classes [9, 10]. Since these nonparametric estimation approaches use some ranking orders rather than actual expression levels, they are more robust to outliers but also lose information about the degree of compactness. As a result, this kind of method separates genes into only a limited number of ranks, which is less sensitive than parametric estimation.

In this paper, a new ranking approach, called weighted punishment on overlap (WEPO), is proposed. WEPO takes advantages of parametric and nonparametric estimations to rank genes sensitively despite the limited number of samples. For each gene, the expression levels of samples are first normalized by using the z-score to eliminate the scaling problem. Then, the samples are sorted according to the normalized expression levels. The punished score of each gene is calculated by estimating the overlapping regions of two classes. Genes with smaller punished scores are considered to be discriminative.

Our approach was tested on three microarray datasets. The support vector machine (LIBSVM) [11] was used to verify the discriminability of the selected genes. We show the robustness and sensitivity of the proposed approach by comparing five well-known feature selection approaches through informative testing, sensitive testing, and significance testing. The experiments show that our method is competitive with these surveyed parametric and nonparametric methods. Genes selected using WEPO are more informative and sensitive than those selected using the surveyed methods both in statistical tests and biological meanings.

The rest of this paper is organized as follows. Section 2 demonstrates the proposed approaches. Section 3 evaluates WEPO based on the results of informative, sensitive, and significance testing. Section 4 discusses the biological meanings by applying WEPO to colon adenocarcinoma data sets and gives conclusions.



2. METHODOLOGY

In this section, the details of the proposed approach, weighted punishment on overlap (WEPO), for gene selection with microarray data are presented. WEPO is based on the assumption that if a gene is differentially expressed between two classes, the expression value of this gene of different groups should come from two quite different distributions. Hence, WEPO scores a gene by estimating the ambiguous region of the expression levels of the samples of two classes to measure the correspondence between the expression levels of a gene and the group membership. For each gene, the expression levels of samples are first normalized by using the z-score to eliminate the problem of scaling. Then, the samples are sorted according to the normalized expression levels. The punished score of each gene is calculated by estimating the overlapping regions of two classes. In the following subsections, the data scaling, sorting, estimating and scoring steps are described.

2.1 Scaling for Comparable Genes

Assume that there are n samples and k genes in the dataset. For gene G_i , $1 \leq i \leq k$, the corresponding gene expression levels in these samples are represented as $(g_{i1}, g_{i2}, \dots, g_{in})$. For each gene, we would like to get a score based on their expression levels. Since the scale of gene expression profiles varies among genes, scaling adjustments are required so that genes can be compared fairly. In this paper, the standardized measurement (z-score) is used to normalize the gene expression profiles:

$$z_{ij} = \frac{g_{ij} - m_i}{\sigma_i}, \quad 1 \leq j \leq n, 1 \leq i \leq k, \quad (1)$$

where σ_i , the mean absolute deviation, is defined as

$$\sigma_i = \frac{1}{n} (|g_{i1} - m_i| + |g_{i2} - m_i| + \dots + |g_{in} - m_i|), \quad (2)$$

and m_i is the mean value of $(g_{i1}, g_{i2}, \dots, g_{in})$, that is,

$$m_i = \frac{1}{n} (g_{i1} + g_{i2} + \dots + g_{in}). \quad (3)$$

2.2 Sorting, Estimating, and Scoring

We assume that there are n samples in two classes, c_1 and c_2 , with n_1 samples in class c_1 and n_2 samples in class c_2 . After the data are normalized, WEPO works as follows to score a gene G_i , $1 \leq i \leq k$. Firstly, two classes of samples are separated (Fig. 1(a)). Then samples in each class are sorted according to the normalized expression levels, Z_{ij} (Fig. 1(b)). For classes c_1 and c_2 , the sorted expression levels of their samples form two expression levels, vector₁ and vector₂. If a gene can be used to discriminate two classes exactly, then vector₁ and vector₂ are non-overlapping. The overlapping region between two vectors represents the ambiguous region between the distributions of two classes.

For example, there are two vectors in Fig. 1(b) for classes c_1 and c_2 , (33, 36, 42, 49, 58, 77, 96) and (1, 6, 17, 25, 38, 44, 69), respectively. If we plot these points in one di-



mension as shown in Fig. 2, then some overlapping region will be found (the shadow part).

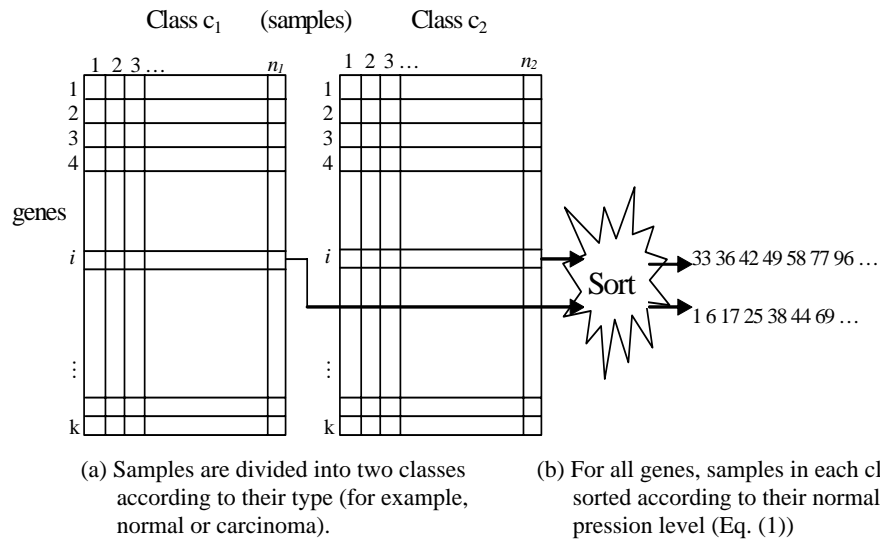


Fig. 1. The first step of WEPO. Samples are separated into two classes according to their labels, for example, normal or disease, as shown in (a). For each gene, samples in each class are sorted based on their normalized expression level (as shown in (b)).

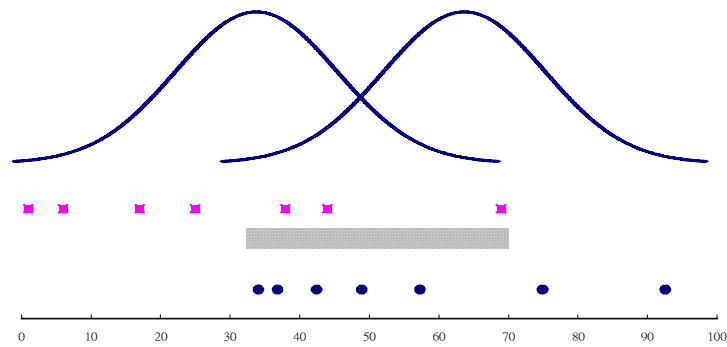


Fig. 2. Two expression level vectors, (33,36,42,49,58,77,96) and (1,6,17,25,38,44,69), from two distributions. The overlap between these two distributions is illustrated by the gray rectangle.

For each point in the ambiguous region, punishment is required to move it to the side of its original group. This punishment is defined as

$$\sum_{p_i \in class_1} \sum_{p_j \in class_2} \Psi(z_{p_j} - z_{p_i}), \quad \Psi(z) = \begin{cases} z, & z > 0 \\ 0, & z \leq 0 \end{cases} \quad (4)$$



This formulation, representing the degree of compactness of two distributions, calculates the weighted sum of the area by using the difference of normalized expression levels. WEPO defines the score of a gene in such way as to rank genes sensitively without losing the information about data distribution. Eq. (4) can be interpreted as swapping, for each element in the second group is exchanged with the elements in the first group that are larger, and the difference between them is summarized.

Fig. 3 shows an example of how WEPO scores a gene with six samples. Class label, $T = \{t_1, t_2, \dots, t_n\}$, represents the labels of samples, where t_i represents the label of the sample i , $t_i \in \{0, 1\}$. Samples are sorted using the z-score (z_{ij}), the normalized expression levels. Base on the sorted class label T , we calculate a score for gene G_i as the minimum swapping penalty of WEPO to arrive at a perfect split, with all the ones in the same category t_i being consecutive in T (Fig. 3(b)(c)). Because genes with smaller scores are more informative, the score for the gene is 4.24625 in this example.

Samples	1	2	3	4	5	6
Expression	45	36	20	174	69	271
z-score	-0.71875	-0.83125	-1.03125	0.89375	-0.41875	2.10625
label	0	1	1	0	1	1
After sorting by z-score						
Samples	3	2	1	5	4	6
z-score:	-1.03125	-0.83125	-0.71875	-0.41875	0.89375	2.10625
label	1	1	0	1	0	1

(a)

swapped score	Class Label	Swapped samples
0.3	110101	1,5
1.2125	111001	4,6
2.825	111010	1,6
	111100	
Total Score		4.24625
Cost for translating to 111100		

(b)

swapped score	Class Label	Swapped samples
1.3125	110101	4,5
0.1125	110011	1,2
1.725	101011	2,4
0.3125	100111	1,3
1.925	010111	3,4
	001111	
Total Score		5.3875
Cost for translating to 001111		

(c)

Fig. 3. An example to demonstrate how WEPO scores a gene. For this gene, there are six samples with their gene expression and label (class 0 or 1). (a) shows the results for the gene expression levels of these samples normalized using the z-score and sorted in increasing order. (b) and (c) show the process of calculating a WEPO score. The calculation steps are sequentially displayed in rows in these tables. The score is the difference between two swapped patients. The total score is the sum of the scores derived in the steps until a perfect split is obtained. There are two ways to arrive at a perfect split in this case. Because genes with smaller scores are more informative, the score for the gene is 4.24625 in this example.



3. EVALUATION

We tested WEPO on three publicly available microarray datasets of cancers (summarized in Table 1) selected from previous studies [1, 2, 12] to show some characteristics of WEPO and to compare WEPO with other methods [3, 7-10]. We will discuss WEPO based on informativeness, sensitivity, and significance. The support vector machine (LIBSVM) [11] was used as a classifier to verify the performance. Firstly, WEPO was compared with five well-known gene selection approaches through the informative testing. Secondly, WEPO was compared with some nonparametric approaches to show its sensitivity. Finally, the statistical p-value was used to verify the significance of the results of WEPO. Experimental results indicate that through WEPO gene selection, SVM can achieve high prediction accuracy. The results of informative testing show that WEPO is comparable with other gene selection methods. WEPO is more sensitive than the surveyed approaches, and genes selected using WEPO are statistical significant.

Table 1. Summary of the three data sets used in the experiment.

Dataset	Adenocarcinoma	Lymphoma	Colon
Publisher	Notterman <i>et al.</i> [12]	Alizadeh <i>et al.</i> [1]	Alon <i>et al.</i> [2]
# of genes	7457	5635	2000
# of samples	18 paired samples (18 “tumor”/ 18 “normal”)	40 samples (19 “GCB”/ 21 “AB”)	62 samples (40 “tumor”/ 22 “normal”)

3.1 Classification – SVM

In this work, a *Support Vector Machine* (SVM) was used as a classifier to verify the performance of the gene selection methods. SVM is a machine learning algorithm proposed by Vladimir Vapnik and his co-workers [13]. It is based on the Structural Risk Minimization principle from statistical learning theory. SVM can be applied to different tasks such as regression, classification, and density estimation. For a binary classification task, given a training set with n class-labeled samples, $(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)$, where x_i is a vector consisting of feature values that represent the i^{th} sample, and $y_i \in \{-1, +1\}$ indicates the class, a SVM classifier learns a linear decision rule, which is represented using a hyperplane R^N . The label of a previously unmarked sample x is determined by which side of the hyperplane x lies on. That is, all the examples on the one side of the hyperplane are labeled positive and the remaining on the other side are labeled negative. The goal of training the SVM is to find a hyperplane that has the maximum margin to separate two classes, as depicted in Fig. 4. For more details on SVM, please see [14, 15]. In the experiment, we used a SVM software package, LIBSVM [11].

3.2 Informative Testing

Informative testing was used to test whether the selected genes were really discriminative of the studied issues. It was difficult to perform “real” informative testing to evaluate



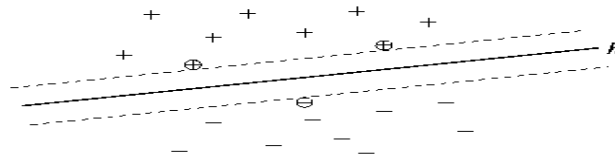


Fig. 4. The basic idea of SVM. + and - denote data of different categories. The solid line represents the hyperplane with the maximum margin for separable data. The examples closest to the hyperplane are called Support Vectors (marked with circles).

the gene selection methods since we didn't know the true status of the genes. One reasonable way to approximate informative testing is to test the effect of the genes on classification accuracy. In this study, SVM was used to perform informative testing. Due to the limited number of samples, leave one out cross validation (LOOCV) was used [9]. In each LOOCV trial with n samples, we sequentially picked up a sample as the test set. The other $n - 1$ samples were treated as the training set. A gene selection method was applied to the training set to provide some selected genes for the SVM classifier to generate a predictor. This predictor was used to predict the class of the sample in the test set. After sequentially picking up n genes, we summarized n prediction results as the classification accuracy of the gene selection method.

Table 2 shows the performance of WEPO when applied to three different cancer datasets. The column "top-ranked genes" lists the top ranking genes selected by WEPO and used in SVM. For example, "1-10" means that SVM used the top ten ranked genes identified by WEPO. Each entry represents the classification accuracy. Among these cancer datasets, the subsets of genes selected using WEPO with sizes smaller than 1000 achieved classification accuracy above 80%. In the Adenocarcinoma and Lymphoma datasets, over 90% of the samples could be correctly predicted.

Table 2. The classification accuracy of three cancer data sets with genes selected by WEPO. The classification accuracy was calculated using LOOCV cross validation (see the text). The column "top-ranked genes" lists the top ranking genes selected by WEPO and used in SVM.

Top-ranked genes	Adenocarcinoma Acc.	Lymphoma Acc.	Colon Acc.
1~10	1	0.925	0.822581
1~50	0.888889	0.95	0.822581
1~100	0.888889	0.95	0.83871
1~200	0.916667	0.95	0.854839
1~300	0.944444	0.95	0.870968
1~400	0.944444	0.925	0.870968
1~500	0.972222	0.925	0.887097
1~600	0.916667	0.925	0.870968
1~700	0.916667	0.925	0.870968
1~800	0.944444	0.925	0.870968
1~900	0.916667	0.925	0.854839
1~1000	0.916667	0.9	0.870968

WEPO was compared with three parametric and two nonparametric feature selection methods based on these datasets by using LOOCV and SVM. Each gene was assigned a unique ranking by using statistical parametric methods, including t-test [7], Fisher [8] and Golub [3]. On the other hand, numbers of genes were appointed the same ranking in two well-known nonparametric methods TNoM [9] and Park [10]. To precisely describe the characteristic features of the nonparametric methods, the average accuracy of the genes with the same nonparametric score were plotted as a dot at the end of their ranking range. Fig. 5 shows the results obtained using these selection methods and the Adenocarcinoma dataset. We got similar results for the other two datasets. As shown, although the behaviors of all the methods are similar, the results of WEPO were slightly better than those of the others. It is noted that WEPO outperformed the others on the points corresponding to fewer genes. This means that WEPO could give higher rankings for more informative genes. Comparing the parametric and the nonparametric approaches, the latter seem perform better than the former in classification accuracy.

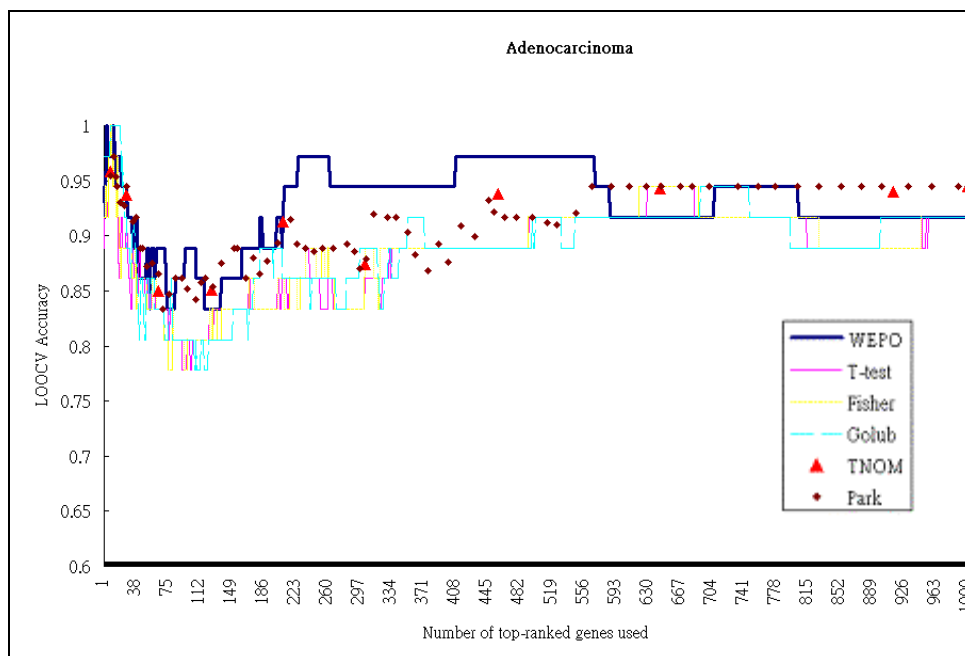


Fig. 5. Comparison of LOOCV classification accuracy between WEPO and five gene selection methods. T-test, Fisher, and Golub are parametric methods. TNoM and Park are nonparametric methods.

3.3 Sensitive Testing

As mentioned above, there were several genes with the same score obtained using the nonparametric methods as shown in Fig. 5. However, we found that genes with the same nonparametric score had different influences on classification accuracy. To interpret



how this characteristic of nonparametric methods may cause slight confusion when selecting informative genes, we performed the following experiment. To calculate accuracy in specifying particular genes, all the samples in Adenocarcinoma dataset are partitioned into training and testing sets, instead of LOOCV. In Fig. 6(a), genes with three Park scores, 8, 18 and 38, are plotted, where the x-axis and y-axis are their WEPO and Park scores, respectively. It is easy to see that genes with the same Park score have different WEPO scores. One score curve, corresponding to one Park scores in Fig. 6(a), overlaps WEPO scores of the one with another Park score. These overlaps imply that the gene selection result for the Adenocarcinoma dataset obtained using Park methods may be quite different from that obtained using WEPO. Fig. 6(b) reveals the testing accuracy of these genes. We find that genes with the same Park score which correspond to a larger range of WEPO scores have greater variance in classification accuracy. Using the Park score in this case may reveal less idea about the goodness of genes within the same Park score class. In comparison, WEPO gives each gene a different score according to its actual expression level. Similar results were obtained for different Park scores and datasets. We think that WEPO is more sensitive than Park in terms of gene ranking.

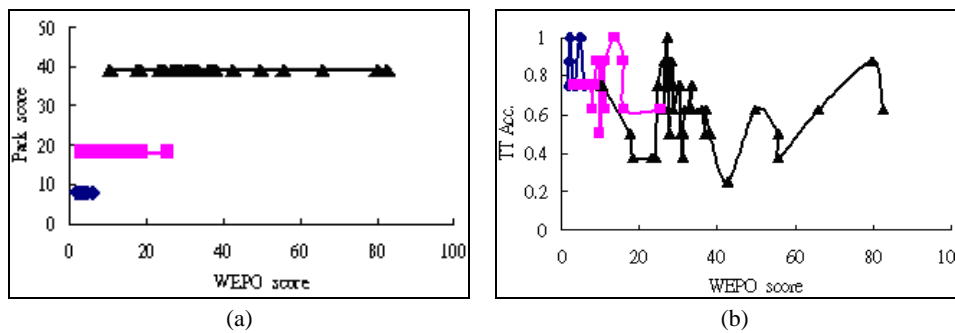


Fig. 6. Some genes in the Adenocarcinoma dataset with Park scores of 8, 18 and 38 are plotted based on: (a) Park score v.s. WEPO score; (b) WEPO score v.s. corresponding classification accuracy. As can be seen, genes with the same Park score which correspond to a larger range of WEPO scores have greater variance in classification accuracy, which means that WEPO is more sensitive than Park in terms of gene ranking in this case.

3.4 Significance Testing

In this study, the significances of genes selected by WEPO were verified. First we examined whether low WEPO score were indicative of the classification of expression. Then a permutation test was performed to show that genes with low WEPO scores were really statistically significant, and that WEPO could select genes highly related to the studied issues.

Observing the relationships between the WEPO scores and expression level of a gene, we found that in most cases, genes with low WEPO scores were indeed indicative of the classification of expression. For example, the two genes *GTF IIIA* and *T49397* in the Adenocarcinoma dataset are plotted in Fig. 7, where the x-axis represents samples, and the y-axis represents expression levels. The first 18 samples on the x-axis are tumor

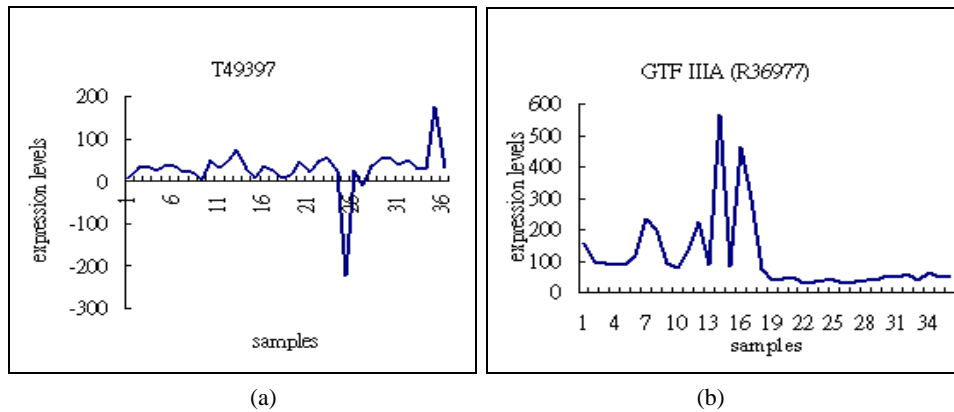


Fig. 7. The expression levels for the two genes *GTF IIIA* and *T49397* in the Adenocarcinoma dataset. There are 36 samples indicated on the x-axis, the first 18 of which are tumors and the remaining are normal. The WEPO scores of *T49397* and *GTF IIIA* are 120 and 0, respectively. The expression level of *GTF IIIA* is uniformly higher for the first 18 samples than for the rest, while there is no difference in the expression levels of *T49397* between the two groups.

tissues, and the remaining ones are normal tissues. The WEPO scores of *T49397* and *GTF IIA* are 120 and 0, respectively. Clearly, there is no difference in the expression levels of *T49397* between two groups. However, the expression profile of *GTF IIIA* has uniformly high expression levels for the first 18 samples and lower levels for the rest. In most cases, genes with lower WEPO scores tend to have different expression levels in the two groups.

To show the statistical significance of the scores obtained by scoring genes in the test dataset, we estimated the probability of getting such results from arbitrary data (p -value). Since there are no simple formulas for deriving null distributions of WEPO scores, a permutation test was adapted to judge whether the results of the Adenocarcinoma dataset were meaningful or accidental. The permutation test compared the distribution of scores from the original cancer data with the null distribution obtained from randomly generated data where genes were independent of the cancer. Due to the biological knowledge that some genes are related in reaction, the correlation structure of the data should be preserved when calculating the null distribution. The simulated null distribution is generated through the following three-steps.

Firstly, 10,000 random configurations of 18 0's and 18 1's representing tumor tissues and normal tissues were generated. Secondly, by assigning 10,000 random configurations to data, we generated random permutations of the entire columns while keeping all the expression levels for each sample together. Finally, the null distribution of WEPO statistics from all genes of these permutations was calculated. By comparing the distribution from the original data with the null distribution, a p -value, the probability of getting such scores from arbitrary data, could be computed.

In Fig. 8(a), we find that p -value increases as the rank of genes increases. The higher the rank of genes, the lower the WEPO score, which implies that lower WEPO score is significant. Fig. 8(b) shows a comparison of the p -values of the WEPO scores from the original data and from one column-permuted data. As observed, the p -values

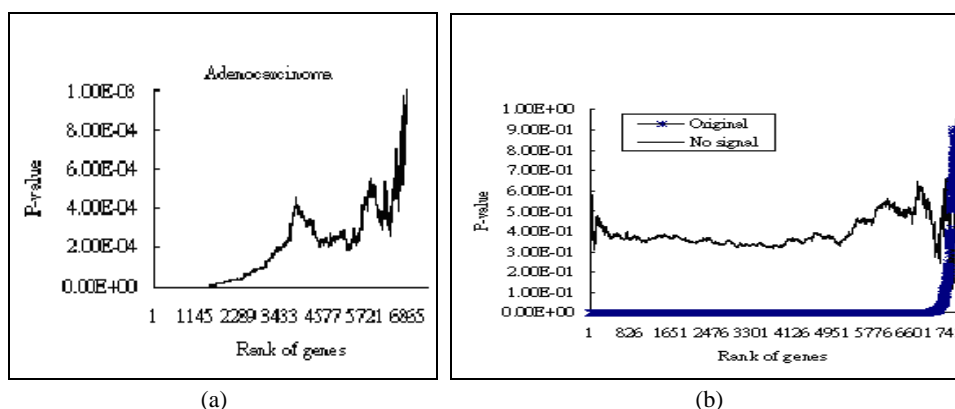


Fig. 8. (a) The p-value of the Adenocarcinoma data increases as an increasing number of top-genes peeled off. The p-values are compared with the 10000 random data. (b) Comparison of p-values between the original Adenoarcinoma data (Original) and the randomly generated data (No signal). The preceding fragment of the p-value curve of the original data is not visible due to the scale of p-value.

from the column-permuted data are much larger than those from the original data, and the p-value curve of the column-permuted data is nearly a horizontal line. Based on previous discussion, we conclude that WEPO can distinguish whether data have signals.

Table 3. Top 10 genes with lowest WEPO score in Adenocarcinoma data set.

Accession no.	Description
R36977	similar to <i>H. sapiens</i> general transcription factor IIIA (GTF IIIA) mRNA
Z50753	<i>H.sapiens</i> mRNA for GCAP-II/uroguanylin precursor
M97496	<i>H.sapiens</i> guanylin mRNA
X64559	<i>H.sapiens</i> mRNA for tetranectin
M77836	Human pyrroline 5-carboxylate reductase mRNA
T96548	similar to <i>H. sapiens</i> action, gamma-enteric smooth muscle
T64297	similar to <i>H. sapiens</i> gb:M10050 fatty acid -binding protein
Z49269	<i>H.sapiens</i> gene for chemokine HCC-1
M83670	Human carbonic anhydrase IV mRNA
H57136	similar to SP:A40533 A40533 cAMP-DEP protein kinase

4. RESULTS AND CONCLUSIONS

We applied WEPO to the Adenocarcinoma dataset analyzed in [12]. Eighteen paired colon adenocarcinoma/normal tissue samples were used to select informative genes. The top 10 genes with the lowest scores are listed at Table 3. Most of these genes are highly related to this disease. As shown in Table 3, a substantial number of transcripts, such as *T64297*, *Z49269*, *M97496*, *T96548*, *X64559*, *Z50753*, *M83670* and *H57136*, were more

highly expressed in normal tissue than in paired cancer specimens. Consistent with [12], many of these transcripts simply represent smooth muscle or connective tissues layers more generously included with the normal than the neoplastic tissue samples. *R36977* and *M77836* were more highly expressed in colonic neoplasia than in normal tissue. According to [12], *R36977* is not associated with colon cancer in previous literature, but is linked to either some forms of neoplasia or to the regulation of the cell cycle. *M77836* is related to altered levels of metabolism (rather than cancer growth *per se*).

This study has demonstrated that WEPO is a robust feature selection approach for microarray data. From our experience, we suggest that a good feature selection method for microarray data should have good mechanisms in order to be robust to outliers and to rank genes sensitively. In our approach, data are normalized using the z-score (sensitive), and genes are scored by estimating the overlapping region of two classes (robust to outliers). Our experiments indicate that genes selected by WEPO are informative, sensitive, and significant.

Experiments conducted on three microarray data verify that the proposed approach is robust and is very competitive with surveyed methods. Specifically, genes selected by WEPO are biologically meaningful. We believe that the robustness of our approach makes it an effective tool for microarray data analysis and potential applications.

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