# Generation of Arbitrary Quadrature-Amplitude Modulated Signals Using a Single Dual-Drive Modulator

Keang-Po Ho

Institute of Communication Engineering and Dept. of Electrical Engineering National Taiwan University, Taipei 106, Taiwan E-mail: kpho@cc.ee.ntu.edu.tw

**Abstract:** Regardless of complexity, all types of quadrature-amplitude modulated (QAM) signal can be generated using a single dual-drive Mach-Zehnder modulator. Three different quadrature phase-shift keying (QPSK) transmitters are proposed as examples.

## I. Introduction

Recently, multilevel modulation schemes like differential quadrature phase-shift keying (DQPSK) have received renewed attention [1]–[4]. Not only for DQPSK or QPSK, but applicable to general class of quadratureamplitude modulation (QAM) with and without differential operation, Fig. 1(a) is the traditional method to generate a QAM signal using two Mach-Zehnder modulators (MZMs) within two  $\pi/2$ -phase difference paths of an Mach-Zehnder interferometer. Intuitively, the two MZMs generate the signal for the two quadrature components with a phase difference of  $\pi/2$ , i.e.,  $\cos(\cdot)$ and  $\sin(\cdot)$ . As shown later, QAM signal can also be generated using a single dual-drive MZM as shown in Fig. 1(b).

## **II.** General Principles

If the two paths of a dual-drive MZM have independent driving voltages of  $V_1$  and  $V_2$ , with an input electric field of  $E_i$ , the output electric field is

$$E_o = \frac{E_i}{2} \left[ \exp\left(j\pi \frac{V_1}{V_{\pi}}\right) + \exp\left(j\pi \frac{V_2}{V_{\pi}}\right) \right], \quad (1)$$

where  $V_{\pi}$  is the voltage to provide a  $\pi$  phase shift of each phase modulator. In additional to operate a MZM



Fig. 1. (a) The traditional QAM transmitter based on two MZMs in an interferometer. (b) A QAM transmitter based on a single dual-drive MZM.

as a phase modulator with  $V_1 = V_2$ , by choosing both  $V_1$  and  $V_2$  of (1) properly, any quadrature signal can be generated. Assumed an *M*-ary signal constellation that can be represented as complex numbers of

$$s_i = r_i e^{j\theta_i}, \quad i = 0, \dots, M - 1,$$
 (2)

with a maximum amplitude of  $r_{\text{max}} = \max\{r_0, r_1, \dots, r_{M-1}\}$ . The input and output relationship of (1) is rewritten in the following normalized form of

$$E_{o} = \frac{r_{\max}}{2} \left( e^{j\phi_{1}} - e^{j\phi_{2}} \right),$$
(3)

where  $\phi_1 = \pi V_1/V_{\pi}$  and  $\phi_2 = \pi V_2/V_{\pi} + \pi$ . The output electric field of  $E_o$  is the difference of two vectors in the circle having a radius of  $r_{\text{max}}/2$ . The MZM of (3) is biased at the minimum transmission point or the null point and the maximum output electric field has an amplitude of  $r_{\text{max}}$  when  $V_1 = V_2$ .

With two phases of [5], [6]

$$\phi_{i1} = \theta_i + \cos^{-1}\left(r_i/r_{\max}\right) \tag{4}$$

$$\phi_{i2} = \theta_i - \cos^{-1}(r_i/r_{\max}) + \pi,$$
 (5)

we obtain

$$s_i = \frac{r_m}{2} \left( e^{j\phi_{i1}} - e^{j\phi_{i2}} \right), \tag{6}$$

because of  $e^{j \cos^{-1} r_i/r_{\text{max}}} + e^{-j \cos^{-1} r_i/r_{\text{max}}} = 2r_i/r_{\text{max}}$ . All constellation points of (2) can be generated based on two phase modulators having the phases of (4) and (5), respectively.

Figs. 2 show a 16-QAM constellation and the phases of (4) and (5) for the dual-drive MZM. Instead of representing all 16 constellation points in the same figure, Fig. 2(a) decomposes the 16-QAM signal into two QPSK and one 8-PSK signals. Figs. 2(b)-(d) are the corresponding  $\phi_{i1}$  and  $\phi_{i2}$  of all 16 points according to the decomposition of Fig. 2(a). The empty and solid circles correspond to  $\phi_{i1}$  and  $\phi_{i2}$ , respectively. Fig. 2(b) gives the QPSK signal of Fig. 2(a) with maximum amplitude of  $r_{max}$ . The two closest points of Fig. 2(b) are the same but draw differently for the phases of two



Fig. 2. (a) 16-QAM constellation and its decomposition into two QPSK and an 8-PSK signals, (b), (c), (d) are the two phases of  $\phi_1$  (empty circles) and  $\phi_2$  (solid circles) to generate the 16-QAM signals.



Fig. 3. (a) QPSK constellation and its generation using a (b) four-, (c) two-, and (d) three-level drive signal.

different signals. Fig. 2(c) generates the 8-PSK signal of Fig. 2(a). Fig. 2(d) gives the QPSK signal of Fig. 2(a) with the smallest amplitude.

From Fig. 2, the generation of a 16-QAM signal using a dual-drive MZM requires the usage of a 16-level drive voltage and thus very complicated drive circuits. Compared with the transmitter of Fig. 1(a), the simplification of the optical components using a single dual-drive MZM creates a high complexity in the electronic circuits. With the allowance of higher modulator loss, as shown later, the number of drive levels can be reduced.

### **III.** Generation of (D)QPSK Signals

The dual-drive MZM transmitter of Fig. 1(b) can use to generate either QPSK or DQPSK signals with a constellation of Fig. 3(a). Similar to that of Fig. 2(b), Fig. 3(b) is the trivial case of operating the dual-drive MZM as a phase modulator with  $V_1 = V_2$ . The four phases of Fig. 3(a) is given by a four-level drive signal. A QPSK signal may be generated with higher loss but smaller number of levels if the four constellation points are generated with phases of  $\phi_1$  or  $\phi_2$  the same as one another. With only two values of  $\phi_1$  and  $\phi_2$ , Fig. 3(c) drives the dual-drive MZM in Fig. 1(b) with a two-level signal. Fig. 3(d) has three different values of  $\phi_1$  and  $\phi_2$ and requires a three-level drive signal. Comparing Figs. 3(c) and (d) with Fig. 3(b), the schemes using two and three level drive signal have 3-dB extra loss than that of



Fig. 4. A RZ-DQPSK transmitter



Fig. 5. The eye-diagram of the drive signal and output intensity between two modulators of the transmitter of Fig. 4 when (a) 4, (b) 3, (c) 2 drive signals are used.

Fig. 3(b). Both the peak-to-peak drive voltage and the number of drive levels are reduced in Figs. 3(c) and (d).

However, both the two- and three-level transmitters of Figs. 3(b) and (c) do not have constant intensity between consecutive symbols. Fig. 4 shows a RZ-DQPSK transmitter using a dual-drive MZM followed by a phase craver. After the phase craver, the intensity is a constant pulse train. However, Figs. 5 show the eyediagram of the drive signal and the intensity before the phase craver. With two or three levels of drive signal, the output intensity of the dual-drive MZM has some ripples between consecutive symbols. The simplest twolevel scheme of Fig. 3(c) and 5(b) has a peaking ripple doubling the output intensity. The two- and three-level drive signals of Fig. 3(c) and (d) are applicable for RZ but not NRZ signals. The peak-to-peak drive voltage is reduced from  $1.5V_{\pi}$  for four-level signal to  $V_{\pi}$  for twoand three-level drive signals.

#### **IV.** Conclusion

Using 16-QAM and QPSK signals as example, we show that a single dual-drive MZM can be used to generate all types of QAM signals.

#### References

- [1] R. A. Griffin et al. OFC '02, paper FD6.
- [2] P. S. Cho et al. IEEE Photon. Technol. Lett. 15, 473 (2003).
- [3] H. Kim and R.-J. Essiambre, *IEEE Photon. Technol. Lett.* 15, 769 (2003).
- [4] N. Yoshikane and I. Morita, OFC '04, paper PDP38.
- [5] D. C. Cox, *IEEE Trans. Commun.* 22, 1942 (1974).
- [6] D. C. Cox and R. P. Leck, IEEE Trans. Commun. 23, 1281 (1975).