

A Parallel Distributed Processing Technique for Job-Shop Scheduling Problems

Chun-Chi Lo, Ching-Chi Hsu¹

Department of Computer Science and Information Engineering
National Taiwan University
Taipei, Taiwan 10764, R.O.C.

Abstract

This paper presents a new parallel distributed processing (PDP) approach to solve job-shop scheduling problem which is np-complete. In this approach, a stochastic model and a controlled external energy is used to improve the scheduling solution iteratively. Different to the processing element (PE) of the Hopfield neural network model, each PE of our model represents an operation of a certain job. So, the functions of each PE are a little more complicated than that of a Hopfield PE. Under such model, each PE is designed to perform some stochastic, collective computations. From experimental result, the solutions can be improved toward optimal ones much faster than other methods. Instead of the polynomial number of variables needed in neural network approach, the variables number needed to formulate a job-shop problem in our model is only a linear function of the operation number contained in the given job-shop problem.

1 Introduction

Job-shop scheduling is an operation sequencing problem on multiple machines subject to some precedence constraints among the operations. In this problem, we have n jobs to be processed through m machines. Each job must pass through each machine exactly once. We call the processing of a job on one machine an "operation". Then, there should be $n * m$ operations in all. Each job should be processed through the machines in a particular order. The order for various jobs can be different because they are assumed to be independent.

From definition [1], a schedule result is *semiactive* if there does not exist an operation which could be started earlier without altering the operation sequence of each machine or violating the precedence constraints and ready dates. An optimal schedule must be semiactive and we often search solutions among the semiactive ones. But the number of semiactive schedule is $(n!)^m$ at all. This makes the search of an optimal solution very hard. Many procedures for solving job-shop scheduling problems have been introduced. They are branch and bound search method, neural network approach, integer programming technique, priority dispatching rules and many other heuristic procedures.

One example of neural network approach was presented by Foo and Takefuji [3] in which job-shop scheduling problem are mapped onto a 2-dimensional Hopfield neural network model. A simulated annealing process is applied to their model in order to avoid local minimal solutions. It suffers from some disadvantages as stated in their paper: the annealing process may take a large amount of time, and this model needs $N = mn(mn + 1)$ number of neurons and N^2 number of interconnections.

We can see that branch and bound methods are very efficient in finding an optimal schedule while the problem size is small and the lower bound is well estimated. In another way, a combination of integer programming technique and neural network was introduced by Foo and Takefuji [4]. It can produce the scheduling result more efficiently by electronic circuit. It is very attractive in the concepts of parallel distributed processing by hardware. From our experiences and the conclusion by Foo and Takefuji [3,4], a

¹Correspondence author

branch and bound approach is practical for small problems, while for a large one, stochastic and mathematical approaches are suggested.

The concepts of our PDP model are similar to that of the stochastic Hopfield neural network model [3] except that each processing element (PE) contains the information about an operation in the job-shop problem and perform a little more complicated functions. The function of every PE are identical. So we have only to define the function that a PE must perform. Aided with an automatically controlled external energy, the PEs will take actions cooperatively so that the schedule solutions are improved step by step.

2 The Parallel Distributed Processing Model

A PDP model processes information through the interaction of a large number of simple processing elements. In our model, each PE represents an operation and contains the information about an operation including ready time, starting time, processing time, etc. Through the interaction with other PEs, each PE will change their own informations and the schedule result will be the final values contained in each PE.

The main ideas of our model include: (1) an automatically controlled external energy is applied to avoid a local optimal solution, (2) each operation must try to swap the sequence order with its preceding operation on the same machine when this action is likely to eliminate the machine idle time between the processing of two adjacent operations. When the machine idle time is reduced, the total completion time of the given jobs will be also reduced. What our model does is to improve a schedule from one solution to another better ones. Thus we will use some heuristics to construct an initial solution and then improve the solutions iteratively toward an optimal one.

To implement the above ideas, we define the actions of each PE to be: (1) compute the priority level of its corresponding operation, and (2) stochastically decide whether to swap the sequencing order with its preceding operation on the same machine according to the current scheduling result. If we swap the operations randomly, there will be little chance to get a good or optimal schedule. If we swap the operations only when it can cause a reduction in the maximal completion time of all the jobs immediately, there will be a lot of local optimal solutions that we can never escape from it. Because of these reason, we define a heuristic for each PE to compute the priority level of its corresponding operation. An operation with higher priority level than its adjacent predecessor on the same machine will have high probability to exchange the order with the predecessor. The priority level is determined according to the current scheduling result. To avoid the local optimal problem, an altering external energy is used to help the search to escape from a local optimal solution and provide the search bound of our PDP model. The external energy will increase step by step and drop to zero when 3 conditions occur: (1) a higher energy mountain than the previous one is climbed, (2) a better solution is found and (3) no better solution is found in an large amount of iterations. When (2) and (3) occur, the height of the energy mountain mentioned in (1) is reset to be zero. The heuristic for computing the priority level and the procedure executed in our PDP model are:

COMPUTE THE PRIORITY VALUE pl_i OF OPERATION o_i

- (1) The default value $pl_i = 0$.
- (2) If the start time of some other successive operation of o_i from the precedence constraint is equal to the finish time of o_i , $pl_i = 1$.
- (3) If the finish time of some other preceding operation of o_i from the precedence constraint is equal to the start time of o_i , $pl_i = -1$.
- (4) If the start time of o_i is equal to its ready time, $pl_i = -2$.
- (5) o_i can not move forward because of precedence constraints and the machine that o_i uses is idle in the time before o_i start, $pl_i = -2$.
- (6) If o_i is in the critical path, $pl_i = 2$.
- (7) If o_i meet more than one of above conditions, the later rule dominate the former ones.

PDP SCHEDULING PROCEDURE

1. Find an initial schedule solution ϕ_0 using some heuristic
2. Compute the energy of ϕ_0 using the function $e_{min} = energy(\phi_0)$
3. $ExtEnergy = 0, StepCount = 0, LongCount = K$.
4. Loop until stopping conditions reached:

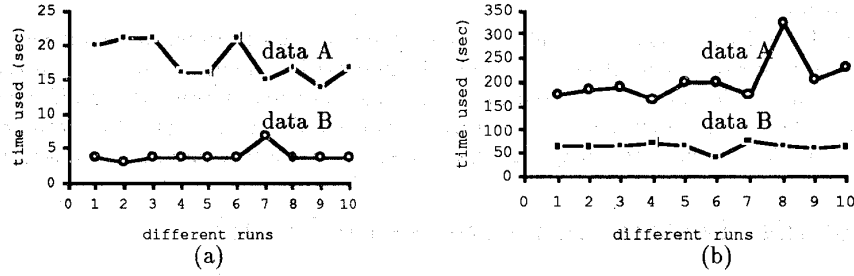


Figure 1: Time needed for (a) two 20-job-4-machine data and (b) two 35-job-5-machine data at a 21 MHz 386 PC

- 4.1 Compute the priority level of each operation under the current solution configuration ϕ_i .
- 4.2 For each operation o_n , take the following actions parallelly and asynchronously
 - 4.2.1 Call *try - move*(o_n) function to try to swap the sequence order with its predecessor o_m on the same machine. If it returns "success", it will generate a new schedule solution ϕ_j . If it return "fail", no change is made to the schedule solution ϕ_i .
 - 4.2.2 If schedule solution changed from ϕ_i to ϕ_j and $energy(\phi_j) < e_{min}$, then $e_{min} = energy(\phi_j)$, record ϕ_j , $ExtEnergy = 0$, $StepCount = 0$, $mountain = e_{min}$.
 - 4.2.3 If $energy(\phi_j) > mountain$, then $mountain = energy(\phi_j)$, $ExtEnergy = 0$, $StepCount = 0$.
 - 4.2.4 $StepCount = StepCount + 1$.
- 4.3 If $StepCount > CountBound$, then $ExtEnergy = 2 * ExtEnergy + 1$, $StepCount = 0$.
- 4.4 If $ExtEnergy > EnergyBound$, then $ExtEnergy = EnergyBound$, $LongCount = LongCount + 1$.
- 4.5 If $LongCount > LongBound$, then $ExtEnergy = 0$, $LongCount = 0$, $mountain = energy(\phi_k)$, where ϕ_k is the schedule solution resulting from 4.2. Goto 4.

The *try - move*(o_n) procedure is used to swap the sequence order of the operation o_n with its preceding operation o_m . But the *try - move* procedure is a stochastic process, i.e., the swapping will not necessarily take place. The probability for the swapping to occur is determined in the following way. If the solution before swapping the order is ϕ_i and the solution after swapping the order is ϕ_j , the probability p_{ij} of moving the schedule from ϕ_i to ϕ_j is:

$$p_{ij} = \begin{cases} \bar{p}_{ij} & \text{if } pl_n > pl_m \\ \rho_1 \cdot \bar{p}_{ij} & \text{otherwise} \end{cases}$$

where \bar{p}_{ij} is defined to be:

$$\bar{p}_{ij} = \begin{cases} 1 & \text{if } energy(\phi_j) \leq energy(\phi_i) \\ \rho_2 & \text{if } energy(\phi_i) < energy(\phi_j) < e_{min} + ExtEnergy \\ 0 & \text{otherwise} \end{cases}$$

where ρ_1 and ρ_2 are constants less than 0.5. We define them to be 0.1 and 0.2 respectively. There are two more point to be mentioned:(1) the swapping of two operation may cause other operation to change their starting time because of the resource conflict, precedence constraint and ready time restriction. Thus, the swapping of operation may cause a global rearrangement of timing, and (2) the lower bound of an optimal job-shop solution can be estimated, so we can stop the PDP procedure until the bound or some time limit are reached.

3 Experimental Result

The data used in our experiment is generated randomly. The operation length is uniformly distributed in a specified range. The processing order of each job on all machines is a random permutation of all the machines. Because the PDP model is a stochastic process, the time need to solve the same problem is not

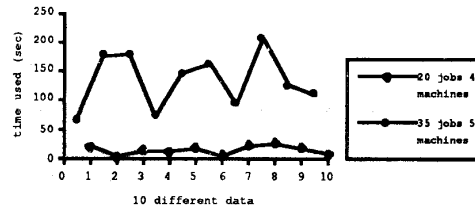


Figure 2: Time needed in one run for different data at a 21 MHz 386 PC

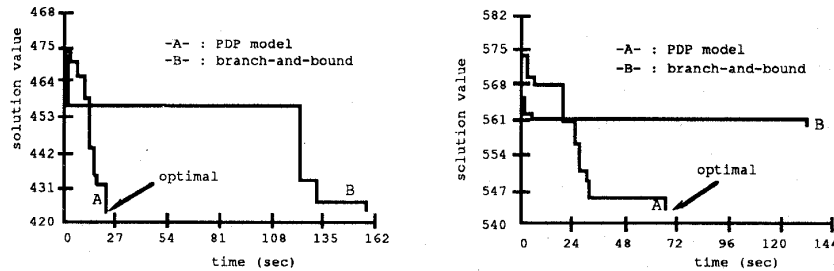


Figure 3: The improvement speed of branch and bound method and our PDP model

the same in different runs. So we experiment each data ten times and list the time needed to find the optimal solutions in figure 1. In addition to it, we generate two sets of data to experiment the time needed to get their optimal solutions. One set contains data of middle size (80 operations) and one contains data of large size (175 operations). Each data is experimented once only. The result is list in figure 2. We also compare our result with the branch and bound approach proposed by Spachis and King [5] and the resulting diagram is illustrated in figure 3.

4 Conclusion

For various kinds of combinatorial optimization problems, when the problem size grow up, traditional dynamic programming, linear programming, branch and bound search and heuristic methods are very hard to find an optimal or near-optimal solution in a reasonable time. For this sake, a parallel distributed processing model aided with some heuristic in each processing element (PE) and working through the cooperative, collective computation is tried to get more opportunity to find an optimal solution in a reasonable time. From the experimental result, the PDP approach give us much encouragement of this idea. Other applications of the PDP model are being researched in our recent works.

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