

# A 2.17-dB NF 5-GHz-Band Monolithic CMOS LNA With 10-mW DC Power Consumption

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**Abstract**—Design principles of CMOS low-noise amplifiers (LNAs) for simultaneous input impedance and noise matching by tailoring device size for  $R_{opt} = 50 \Omega$  are introduced. It is found that  $R_{opt}$  close to  $50 \Omega$  can be obtained by using small devices ( $110 \mu\text{m}$ ) and small currents (5 mA). Based on the proposed approach, CMOS LNAs with on-chip input and output matching networks on thin ( $\sim 20 \mu\text{m}$ ) and normal ( $750 \mu\text{m}$ ) substrates are implemented. It is found that the noise figure (NF) (3.0 dB) of the CMOS LNA at 5.2 GHz with 10-mW power consumption on the normal ( $750 \mu\text{m}$ ) substrate can be reduced to 2.17 dB after the substrate is thinned down to  $\sim 20 \mu\text{m}$ . The reduction of NF is attributed to the suppression of substrate loss of the on-chip inductors. The input return loss ( $S_{11}$ ) is smaller than  $-22$  dB across the entire band of interest (5.15–5.35 GHz). An input 1-dB compression point ( $P_{1\text{dB}}$ ) of  $-8.3$  dBm and an input third-order intercept point of 0.8 dBm were also obtained for the LNA on the thin substrate.

**Index Terms**—Low-noise amplifier (LNA), MOSFET amplifier, noise figure (NF), thin substrate.

## I. INTRODUCTION

HIGH data-rate (up to 50 Mb/s) wireless local area networks (LANs), which exploit the 300-MHz bandwidth in the 5-GHz frequency band (5.15–5.35/ 5.725–5.825 GHz) released by the Federal Communications Commission (FCC) for the unlicensed national information infrastructure (UNII) have become increasingly popular and important for mobile computing devices such as notebook computers. The allocated frequencies overlap the European standard for the high-performance radio local area network (HIPERLAN), which also operates in the 5-GHz band (5.15–5.35/5.47–5.725 GHz). Recently, many *C*-band low-noise amplifiers (LNAs) have been implemented in various technologies for these LAN systems with excellent noise performance [1]–[14]. However, some of the LNAs with extremely low noise figures (NFs) were achieved at the expense of very high dc power consumption, and others suffered from high input/output return losses ( $> -10$  dB), insufficient dynamic range ( $P_{1\text{dB}} < -20$  dBm),

or low linearity [input third-order intercept point (input IP3)]. Ultra-low NF is generally not necessary in short-range wireless applications, while low power dissipation to extend the battery life is strongly demanded for portable wireless data applications [5]. Table I is a summary of recent reports on *C*-band LNAs with low dc power consumption ( $< 15$  mW). From Table I, it is clear that CMOS integrated circuits, which are receiving much attention due to their potential for low cost and the prospect of system-level integration [15], must equal to or surpass the low power consumption ( $\sim 10$  mW) and low NF ( $< 3.0$  dB) of the bipolar and GaAs circuits in order to compete with them. Besides, as previously mentioned, good input/output match, sufficient linearity, and high dynamic range are required as well. In commercial and consumer applications, the cost must also be kept low. One solution to this is the use of a foundry process with proven yield and reliability to fabricate the circuits with on-chip input/output matching networks.

Therefore, there is a need to implement an LNA, which can simultaneously balance all of the following constraints:

- 1) low NF ( $< 3.0$  dB);
- 2) low dc power consumption ( $< 15$  mW);
- 3) low input/output return losses ( $< -10$  dB);
- 4) sufficient input  $P_{1\text{dB}}$  ( $> -20$  dBm);
- 5) high input IP3 ( $> -10$  dBm);
- 6) low cost.

In this paper, we describe 5-GHz-band CMOS LNAs on both thin ( $\sim 20 \mu\text{m}$ ) and normal ( $750 \mu\text{m}$ ) substrates, which meet all the above requirements. The purpose of silicon substrate thinning of the LNA is to study the effect of silicon substrate thickness on the NF performance. The emphasis of this study is to reduce the power consumption of the CMOS LNA while still retaining acceptable noise performance, good input/output match, sufficient linearity, and a high dynamic range. A single-stage cascode amplifier topology with inductive degeneration at the source was used. In the course of developing such an LNA, a formula of the NF for a field-effect transistor (FET) with source and gate inductors was derived to facilitate circuit design. Based on the derived formula and the careful selection of the device size and bias, the gate inductor and source inductor, a CMOS on-chip matched LNA with a normal ( $750 \mu\text{m}$ ) substrate for 802.11a and HIPERLAN2 receivers exhibiting NFs of 2.7, 3.0, and 3.3 dB, input return losses of  $-27$ ,  $-30$ , and  $-29$  dB, output return losses of  $-15$ ,  $-15$ , and  $-16$  dB,  $P_{1\text{dB}}$  of  $-8.36$ ,  $-8.3$ , and  $-8.33$  dBm, input IP3 of 0.3, 0.3, and 0.4 dBm with power consumptions of 12, 10 and 3.6 mW, respectively, were demonstrated experimentally (see Table I). In addition, it was found that the NF (2.17 dB) of the LNA with power consumption of 10 mW on a thin substrate ( $20 \mu\text{m}$ ) was better than that (3 dB)

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TABLE I  
SUMMARY OF THE STATE-OF-THE-ART C-BAND LNAs

References	$f_c$	NF	Gate Length	$P_{DC}$	Gain	input return loss	output return loss	IIP3	$P_{1dB}$ (input)
	(GHz)	(dB)	( $\mu\text{m}$ )	(mW)	(dB)	(dB)	(dB)	(dBm)	(dBm)
This Work (CMOS, Before Thinning Down)	5.2	3.3	0.25	3.6	8.0	-29	-16	0.4	-8.33
	5.2	3.0	0.25	10	10	-30	-15	0.3	-8.3
	5.2	2.7	0.25	12	11.5	-27	-15	0.3	-8.36
This Work (CMOS, After Thinning Down)	5.2	2.17	0.25	10	11	-45	-15	0.3	-8.3
MESFET[4]	5.5	3.5	0.7	9.9	14.85	na	na	na	-21
MESFET[5]	5	1.9	0.6	13.2	10.9	-21	-10	5	na
MESFET[6]	5	1.8	0.6	6	16.5	-16	-4	-6	-16
SiGe HBT[7]	5.8	2.1*	0.5 $\times$ 10 (emitter)	13	13	-6	-4	-10.5	-21
CMOS[8]	5	4.8	0.24	7.2	18 <sup>+</sup>	-12	na	na	na
CMOS[9]	5.25	5.3	0.25	6	6.8	-10.4	-11.6	-3.5	3.3
	5.25	3.5	0.25	12	11.6	-10.9	-12.4	-1.5	-8.7
	5.25	2.5	0.25	48 <sup>++</sup>	16	-12.3	-11.9	-1.5	-11.7
CMOS[10]	5.2	2.1	0.25	9	17	-10	na	na	na
CMOS[11]	5.25	4.5	0.35	10	15.5 <sup>+</sup>	-15	na	5.6	-1.5
CMOS[12]	5.75	1.8**	0.18	21.6 <sup>++</sup>	14.1	-11	-11	4.2	0
CMOS[13]	5.2	2.45	0.35	26.4 <sup>++</sup>	19.3	na	na	-6.1	na

\*: input off-chip matching; \*\*: input off-chip matching & dual-gate layout  
+: voltage gain; ++:  $P_{DC} > 15$  mW

of the LNA on a normal substrate (750  $\mu\text{m}$ ) [16]. The reduction of the NF of an LNA with a thin substrate is mainly due to reduction of the substrate loss of the inductors in the LNA.

## II. PRINCIPLES OF CIRCUIT DESIGN

The schematic of the popular source–inductor–feedback amplifier with the gate inductor for input impedance matching is shown in Fig. 1(a). Fig. 1(b) shows an equivalent circuit of Fig. 1(a) for noise calculation. The source inductor  $L_S$  is used to achieve simultaneous input and noise matching [15]–[18] and to provide the desired input resistance (50  $\Omega$ ) [19]. To thoroughly understand the effect of source inductance on the NF of an FET quantitatively, a formula of the NF for an FET with source and gate inductors was derived and is detailed as follows.

### A. NF of an FET With Source and Gate Inductors

By extending the noise theory for an FET *without* a source inductor published by Pucel *et al.* [20] and referring to Fig. 1(b), we have derived the NF  $F$  for an FET *with* source and gate inductors as follows:

$$F = 1 + \frac{1}{R_S} \left\{ R_g + R_{\ell g} + R_{\ell f} + R_f + |Z_t|^2 \frac{\overline{i_g^2}}{4kT\Delta f} + \left| \frac{1 + j\omega C_{gs} Z_t}{g_m} \right|^2 \cdot \frac{\overline{i_d^2}}{4kT\Delta f} - 2\text{Re} \left[ Z_t \left( \frac{1 + j\omega C_{gs} Z_t}{g_m} \right)^* \frac{\overline{i_g^* i_d}}{4kT\Delta f} \right] \right\} \quad (1)$$

where  $R_S$  is the signal source resistance (usually 50  $\Omega$ ),  $R_g$  and  $R_f$  represent gate and source parasitic resistances of the FET,

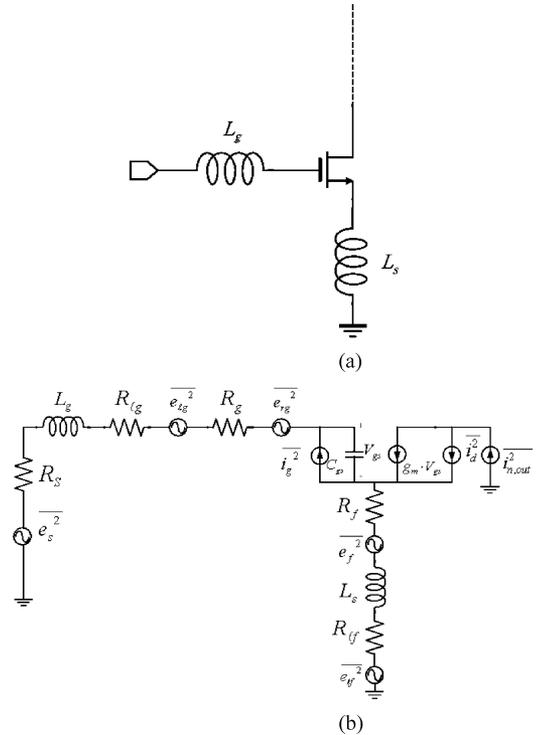


Fig. 1. (a) Schematic of the popular source–inductor–feedback amplifier with an input matching gate inductor. (b) Equivalent circuit of Fig. 1(a) for noise calculation.

respectively,  $R_{\ell g}$  and  $R_{\ell f}$  stand for the series resistance of the inductors  $L_g$  and  $L_S$ , respectively,  $Z_t = Z_S + R_g + R_f + R_{\ell g} + R_{\ell f} + j\omega(L_g + L_S)$ ,  $Z_S$  is the source impedance of the signal source,  $g_m$  is the transconductance of the FET,  $C_{gs}$  is

the gate-to-source capacitance of the FET,  $k$  is the Boltzmann constant,  $T$  is absolute temperature,  $f$  is frequency,  $i_g$  is the induced gate noise current, and  $i_d$  is the drain noise current. Re denotes “the real part of.”

$i_g$  and  $i_d$  can be written as

$$\overline{|i_g^2|} = R \frac{\omega^2 C_{gs}^2}{g_m} 4kT\Delta f \quad (2)$$

$$\overline{|i_d^2|} = P g_m 4kT\Delta f \quad (3)$$

where  $R$  and  $P$  are the coefficients of gate and drain noise, respectively, and are equal to  $(\delta \cdot \alpha)/5$  and  $\gamma/\alpha$  if the symbols in [21] and [22] are used, where  $\delta$  is the coefficient of gate noise,  $\gamma$  is the coefficient of drain noise, and  $\alpha$  is the ratio of device transconductance to zero-bias drain conductance.

In fact, the expression for  $F$  can be put in the following useful form by inserting (2) and (3) into (1):

$$F = 1 + \frac{R_u + G_n |Z_S + Z_C|^2}{R_S} \quad (4)$$

where  $R_u$ ,  $G_n$ , and  $Z_C$  are defined as follows:

$$R_u \equiv R_g + R_{\ell g} + R_{\ell f} + R_f + \frac{K_r}{g_m} \quad (5)$$

$$G_n \equiv K_g \frac{\omega^2 C_{gs}^2}{g_m} \quad (6)$$

$$Z_C \equiv R_C + jX_C = R_g + R_{\ell g} + R_{\ell f} + R_f + \frac{K_C}{j\omega C_{gs}} + j\omega(L_g + L_S). \quad (7)$$

Comparing (5)–(7) with (35)–(37) derived in the Appendix, it can be seen that  $K_g$ ,  $K_C$ , and  $K_r$  are the functions of  $P$ ,  $R$ , and  $C$  as follows:

$$K_g = P \left[ \left(1 - C\sqrt{\frac{R}{P}}\right)^2 + \frac{(1 - C^2)R}{P} \right] \quad (8)$$

$$K_C = \frac{1 - C\sqrt{\frac{R}{P}}}{\left(1 - C\sqrt{\frac{R}{P}}\right)^2 + \frac{(1 - C^2)R}{P}} \quad (9)$$

$$K_r = \frac{\frac{(1 - C^2)R}{P}}{\left(1 - C\sqrt{\frac{R}{P}}\right)^2 + \frac{(1 - C^2)R}{P}}. \quad (10)$$

$C$  is the correlation coefficient of  $i_g$  and  $i_d$  defined by

$$jC = \frac{\overline{i_g^* i_d}}{\sqrt{\overline{|i_g^2|}} \cdot \sqrt{\overline{|i_d^2|}}}. \quad (11)$$

Theoretically, the value of  $C$  is 0.395 for a long channel device [21]. Since  $R$  and  $P$  are difficult to extract from the measured results, we shall consider these  $K$  functions as our fundamental noise coefficients, which can be estimated from the measured noise parameters ( $R_{\text{opt}}$ ,  $X_{\text{opt}}$ ,  $F_{\text{min}}$ , and  $R_n$ ), as will be described shortly. The expression of NF  $F$  in (4) is usually written in terms of minimum NF  $F_{\text{min}}$ , and the optimal source impedance  $Z_{\text{opt}} = R_{\text{opt}} + jX_{\text{opt}}$  or source admittance  $Y_{\text{opt}} = G_{\text{opt}} + jB_{\text{opt}}$  as follows:

$$F = F_{\text{min}} + \frac{G_n}{R_S} |Z_S - Z_{\text{opt}}|^2 \quad (12)$$

$$= F_{\text{min}} + \frac{G_n}{R_S} |Z_S - R_{\text{opt}} - jX_{\text{opt}}|^2 \quad (13)$$

$$= F_{\text{min}} + \frac{R_n}{G_S} |Y_S - G_{\text{opt}} - jB_{\text{opt}}|^2 \quad (14)$$

where  $R_{\text{opt}}$ ,  $X_{\text{opt}}$ ,  $F_{\text{min}}$ , and  $R_n$  are given by (15)–(19), shown at the bottom of this page. Now, several observations are described in order here. For the time being, let us suppose that  $L_g = 0$ . From (18), we know that the introduction of  $L_S$ , to a first-order approximation, does not affect  $F_{\text{min}}$ , which is consistent with the experimental results [23]. According to (15) and (17), it is also interesting to note that  $R_{\text{opt}}$  is independent of  $L_S$ , while  $X_{\text{opt}}$  is reduced when  $L_S$  is introduced; i.e.,  $Z_{\text{opt}}$  in the Smith chart should follow a constant resistance ( $R_{\text{opt}}$ ) circle with decreasing reactance ( $X_{\text{opt}}$ ) when  $L_S$  increases, as shown in Fig. 2(a), which, to a first-order approximation, agrees

$$R_{\text{opt}} = \sqrt{R_C^2 + \frac{R_u}{G_n}} \quad (15)$$

$$\begin{aligned} &= \sqrt{(R_g + R_{\ell g} + R_{\ell f} + R_f)^2 + \frac{(R_g + R_{\ell g} + R_{\ell f} + R_f)g_m}{K_g \omega^2 C_{gs}^2} + \frac{K_r}{K_g \omega^2 C_{gs}^2}} \\ &= \sqrt{(R_g + R_{\ell g} + R_{\ell f} + R_f)^2 + \frac{(R_g + R_{\ell g} + R_{\ell f} + R_f)\omega_T^2}{K_g g_m} + \frac{K_r \omega_T^2}{K_g g_m^2}} \end{aligned} \quad (16)$$

$$\begin{aligned} X_{\text{opt}} &= -X_C \\ &= \frac{K_C}{\omega C_{gs}} - \omega(L_g + L_S) \end{aligned} \quad (17)$$

$$F_{\text{min}} = 1 + 2G_n (R_C + R_{\text{opt}}) \quad (18)$$

$$\begin{aligned} R_n &= R_u + G_n |Z_C|^2 \\ &= G_n (R_{\text{opt}}^2 + X_{\text{opt}}^2) \end{aligned} \quad (19)$$

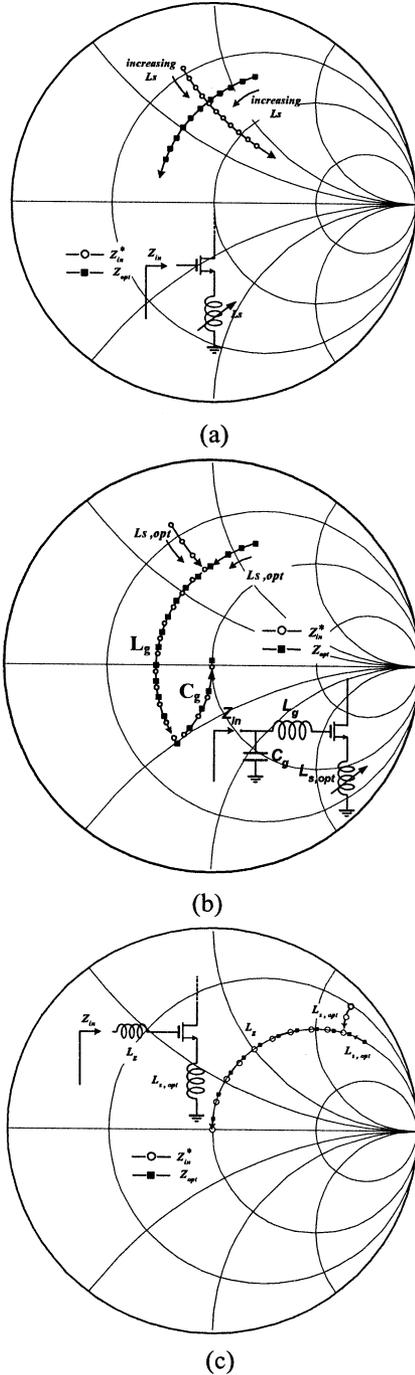


Fig. 2. Loci of  $Z_{\text{opt}}$  and  $Z_{\text{in}}^*$  in the Smith chart with increasing  $L_g$  and  $L_s$ . (a) To a first-order approximation,  $Z_{\text{opt}}$  follows a constant resistance circle with decreasing reactance ( $X_{\text{opt}}$ ) when  $L_g$  and  $L_s$  are increased and the loci of  $Z_{\text{opt}}$  and  $Z_{\text{in}}^*$  intercept at some point. (b) The loci of  $Z_{\text{opt}}$  and  $Z_{\text{in}}^*$  in the Smith chart with  $L_g$ ,  $C_g$ , and  $L_s$ . (c) The loci of  $Z_{\text{opt}}$  and  $Z_{\text{in}}^*$  in the Smith chart with  $L_g$  and  $L_s$  when  $R_{\text{opt}} = 50 \Omega$  is required.

with the published experimental data [17]. On the other hand, the input impedance  $Z_{\text{in}}$  of the LNA is given by

$$Z_{\text{in}} = R_g + R_{\ell g} + R_{\ell f} + R_f + \frac{g_m L_S}{C_{\text{gs}}} + \frac{1 + g_m R_f}{j\omega C_{\text{gs}}} + j\omega(L_g + L_S) \quad (20)$$

if gate-to-drain capacitance ( $C_{\text{gd}}$ ) and output resistance ( $R_o$ ) of the FET are neglected (and, correspondingly, the termina-

tion condition applied to the drain is immaterial). The locus of the complex conjugate of the input impedance  $Z_{\text{in}}^*$  with increasing  $L_S$  is also shown in Fig. 2(a). The two loci intercept at some point, which stands for the simultaneous impedance and noise matching if  $K_c = 1$  and if a suitable source inductor  $L_{S,\text{opt}}$  is chosen. Note that, if  $K_c \neq 1$ , it is impossible to achieve impedance matching and noise matching simultaneously. Therefore, it is important for a circuit designer to check whether the  $K_c$  of the CMOS process that will be used is close to 1 or not before the source inductor feedback technique can be used for simultaneous input and noise matching. We will discuss the value of  $K_c$  later. For the time being, if we assume  $K_c = 1$ , then a matching network consisting of  $L_g$  and  $C_g$  can be used to transform the signal source impedance (usually  $50 \Omega$ ) into this intercept point, as shown in Fig. 2(b). For the ease of matching, one may even eliminate the need of  $C_g$  if  $Z_{\text{opt}} = R_{\text{opt}} + jX_{\text{opt}}$  is chosen to be  $50 \Omega + j0 \Omega$ . According to (15), it is doable to modify  $R_{\text{opt}}$  by a careful selection of transistor size ( $C_{\text{gs}}$ ) and transconductance ( $g_m$ ) or bias.  $L_{S,\text{opt}}$  is then selected so that  $\text{Re}(Z_{\text{in}}) (\sim g_m L_{S,\text{opt}}/C_{\text{gs}})$  is also  $50 \Omega$  and  $Z_{\text{opt}}$  and  $Z_{\text{in}}^*$  are coincident at a point on the constant  $50\text{-}\Omega$  circle in the Smith chart. Nevertheless, from (17), it is, in general, not possible to reduce  $X_{\text{opt}}$  to zero by merely changing transistor parameters or by the use of  $L_{S,\text{opt}}$ . Hence, a gate inductor  $L_g$  must be added to reduce  $X_{\text{opt}}$  to zero in order to achieve the minimum NF condition ( $Z_{\text{opt}} = 50 \Omega + j0 \Omega$ ). The loci of  $Z_{\text{in}}^*$  and  $Z_{\text{opt}}$  corresponding to this situation are shown in Fig. 2(c). Also note that when  $X_{\text{opt}} (= -X_c)$  is reduced,  $R_n$  is reduced as well according to (19). However, one must be cautious that  $L_g + L_S$  should not be too large or  $X_{\text{opt}}$  may become negative, and both the NF and  $R_n$  will increase accordingly.

## B. Design Procedure of the Source-Inductor-Feedback LNA

Suppose that an LNA in an RF receiver is preceded by a high-frequency bandpass filter whose output resistance is  $50 \Omega$ , then  $Z_S = 50 \Omega + j0 \Omega$ . As previously mentioned,  $R_{\text{opt}}$  has to be  $50 \Omega$  and  $X_{\text{opt}}$  has to be zero in order to achieve the minimum NF  $F_{\text{min}}$  if we want to avoid additional input matching components other than  $L_g$ . According to (15),  $R_{\text{opt}}$  can be set to  $50 \Omega$  by choosing suitable  $g_m$  and  $C_{\text{gs}}$  if  $K_g$  and  $K_r$  are known. Similarly,  $X_{\text{opt}}$  can be reduced to zero by choosing suitable  $L_g + L_S$  if  $K_c$  is given.  $K_g$ ,  $K_c$ , and  $K_r$  can be estimated from the measured  $R_n$ ,  $R_{\text{opt}}$ , and  $X_{\text{opt}}$  of an FET without source and gate inductors (i.e.,  $L_g = L_S = R_{\ell g} = R_{\ell f} = 0$ ) based on the following proposed steps. First of all,  $G_n$  can be determined by (19). Second,  $K_g$  can be determined by (6). Third,  $K_r$  can be determined by (16). Finally,  $K_c$  can be determined by (17).  $K_g$ ,  $K_c$ , and  $K_r$  were estimated from a test device before the design of the LNAs studied in this paper. It is found that  $K_g$ ,  $K_c$ , and  $K_r$  are weak functions of frequency [see Fig. 3(a)]. In addition,  $K_c$  is 1 within an experimental uncertainty. Therefore, at least for the current CMOS process, impedance matching and noise matching can be achieved simultaneously. Besides, as shown in Fig. 3(b)–(d), the agreements between the predicted and experimental values of  $R_{\text{opt}}$ ,  $X_{\text{opt}}$ , and  $F_{\text{min}}$  are quite satisfactory for the design of LNAs.

As mentioned before, in an average modern CMOS process, whether  $K_c$  is always close to 1 or not is crucial. From (9),  $K_c$  is

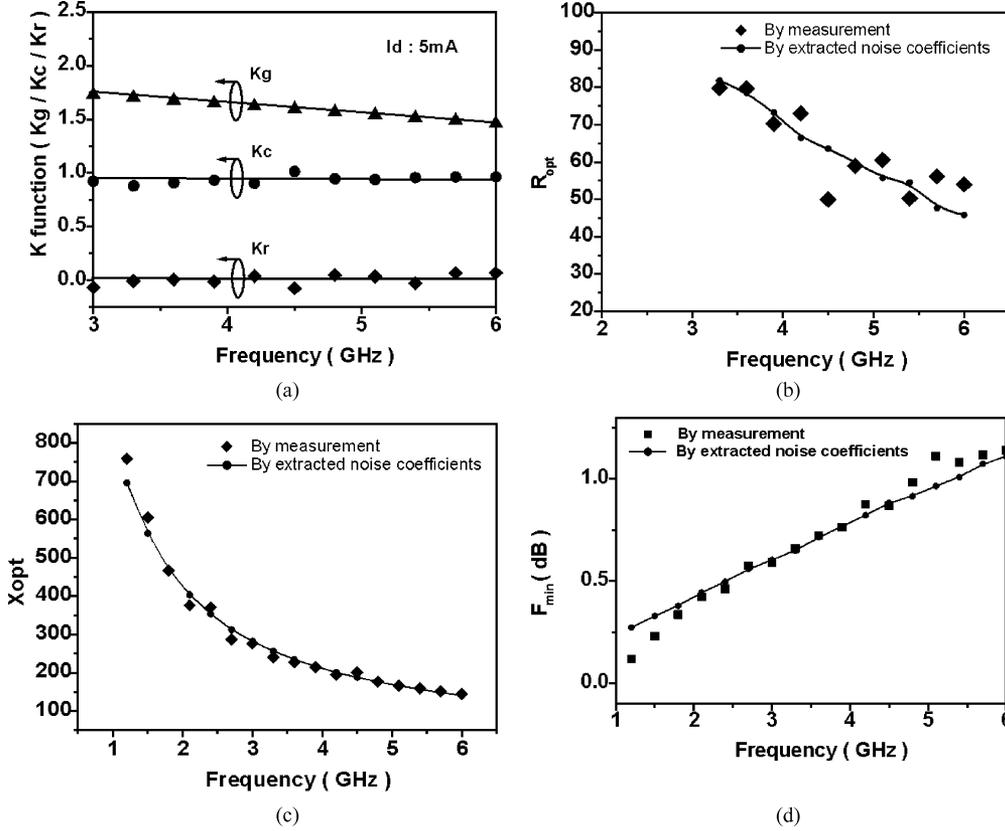


Fig. 3. (a) Extracted  $K_g$ ,  $K_c$ , and  $K_r$  versus frequency characteristics of a MOSFET *without* source and gate inductors (i.e.,  $L_g = L_S = R_{\ell g} = R_{\ell f} = 0$ ). (b) Comparison between predicted and experimental  $R_{opt}$ . (c) Comparison between predicted and experimental  $X_{opt}$ . (d) Comparison between predicted and experimental  $F_{min}$ .

a function of the ratio  $R/P$ , and  $C$ . Since  $C$  in the short-channel regime is not currently known, we have assumed  $C$  to be equal to its long channel value (i.e., 0.395), as was done in [22]. The values of  $K_c$  versus  $R/P$  based on (9) are plotted in Fig. 4. From this figure, it is clear that when  $R/P$  is beyond 0.042,  $K_c$  is a monotonically decreasing function of  $R/P$ . Since the ratio  $R/P$  can be interpreted physically as the relative contribution of gate noise and drain noise to the total noise, we may say that  $K_c$  deviates from 1 substantially if the gate noise plays an important role in a device. Some specific values of  $R/P$  ( $= 0.2 \cdot (\delta/\gamma)^2 \cdot \alpha^2$ ) may be given to get a feeling of the values of  $K_c$ . For a long-channel FET,  $\gamma = 2/3$  and  $\delta = 4/3$  (twice  $\gamma$ ) [21]. For a short-channel device, the assumptions made in [22] are adopted, i.e.,  $\delta$  continues to be approximately twice as large as  $\gamma$  and, hence, although  $\gamma$  and  $\delta$  are taken as 1–2 and 2–4, respectively, the ratio  $\delta/\gamma$  is still a constant 2. Now  $K_c$  is only a function of  $\alpha$ . If  $\alpha = 1$  and  $\alpha = 0.85$  were used for long- and short-channel devices [22], respectively, then the calculated ratio  $R/P$  can be summarized as

$$\frac{R}{P} = \frac{1}{5} \cdot \left(\frac{\delta}{\gamma}\right)^2 \cdot \alpha^2 = 0.4 \cdot \alpha^2 = \begin{cases} 0.4 & \text{(long channel)} \\ 0.289 & \text{(short channel)} \end{cases} \quad (21)$$

From (21) and Fig. 4, the corresponding  $K_c$  is 0.833 and 0.911 for long- and short-channel devices, respectively. Therefore, for an average modern CMOS process,  $K_c$  should be close to 1. In addition,  $K_g$ ,  $K_c$ , and  $K_r$  are functions of  $R/P$  and  $C$  from (8)–(10). If  $C$  is assumed to be equal to its long channel value

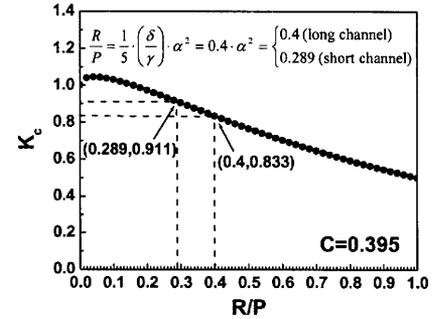


Fig. 4. Calculated  $K_c$  versus  $R/P$  characteristics of modern CMOS technologies.

(i.e., 0.395), then  $\alpha$  (the indication of the gate length) is the only parameter that most strongly affect the values of the three  $K$ -parameters, i.e., process parameters highly related to gate length ( $L_g$ ) will most strongly affect the values of the three  $K$ -parameters.

The complete schematic of our LNA is shown in Fig. 5. A single-stage topology is chosen to minimize the power dissipation and to improve input 1-dB compression point ( $P_{1\text{ dB}}$ ) and input IP3 [15]. A cascode configuration is used to improve stability and to reduce the Miller effect. The source inductor  $L_S$  is used for simultaneous input and noise matching, while inductors  $L_1$  and  $L_2$  and capacitor  $C_{out}$  are used for output matching.

Fig. 6 presents a flowchart of the design procedures for finding the size and bias of the transistor. First, the current density  $J_C$  [or gate overdrive voltage ( $V_{GS} - V_T$ )] and current

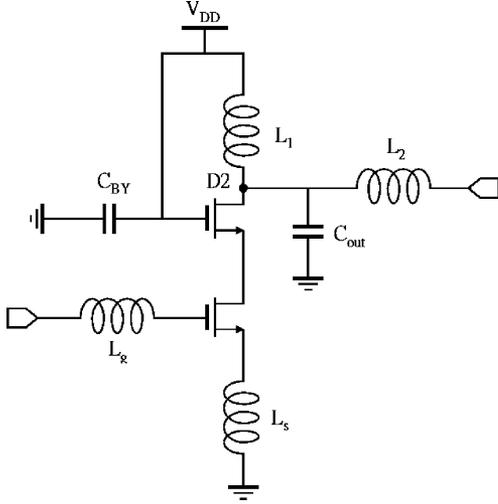


Fig. 5. Complete schematic of the LNA.

gain cutoff frequency  $f_T$  of the transistor are set to the values corresponding to the minimum  $F_{\min}$  of the test device. As shown in Fig. 7,  $J_C$  and  $f_T$  corresponding to the minimum  $F_{\min}$  (1.0 dB) of the test device are  $49 \mu\text{A}/\mu\text{m}$  and 26 GHz, respectively. Second, check if  $S_{21}$  meets the specification, which is set to 10 dB. If yes, go to the next step. If no, return to the first step, i.e., sacrifice  $F_{\min}$  in order to make  $S_{21}$  meet the specification. It can be shown that  $S_{21}$  of the LNA is given by

$$S_{21} = \frac{\omega_T}{\omega_O} \sqrt{\frac{R_P}{R_S}} \quad (22)$$

where  $\omega_O = 1/\sqrt{(L_g + L_s)C_{gs}}$  is the resonant frequency of the input/output matching networks and  $R_P$  is the resistance seen at point D2 at the resonant frequency. Since  $R_P$  is not known *a priori*, a conservative and worse case value of  $50 \Omega$  is chosen for the initial estimate of  $S_{21}$ . Third, for noise matching,  $R_{\text{opt}}$  is set to  $50 \Omega$  and, from (16), the required  $g_m$  can be decided. Fourth, the required  $W$  is decided by  $g_m$  and  $f_T$ . Fifth, the driving current  $I_C$  is decided by  $J_C$  and  $W$ . Finally, if the power consumption and linearity meet the specification, then the finding of the size and bias of the transistor is completed. Otherwise, go back to step 1 and use lower current density.

After deciding the size and bias of the transistor, the other components of the LNA can be determined as follows. The input resistance  $R_{\text{in}}$  of the LNA is known to be  $R_{\text{in}} = \omega_T L_S$  [19] and, thus,  $L_S$  is determined when  $R_{\text{in}}$  is set to  $50 \Omega$ .  $L_g$  is calculated by setting (17), i.e.,  $X_{\text{opt}}$  to zero.  $L_1$ ,  $L_2$ , and capacitor  $C_{\text{out}}$  are determined by the standard matching technique. The calculated result shows that the best condition is  $W = 110 \mu\text{m}$  and  $I_C = 5 \text{ mA}$  for  $R_{\text{opt}} = 50 \Omega$ . The measured result shows that  $R_{\text{opt}} = 44 \Omega$  is achieved when  $W = 110 \mu\text{m}$  and  $I_C = 5 \text{ mA}$ , which not only agree with the calculated results, but also experimentally demonstrate that  $R_{\text{opt}}$  close to  $50 \Omega$  can be obtained by using small device and small current and, therefore, the power constraint method [19], [22] is not always necessary.

### III. CIRCUIT IMPLEMENTATION AND MEASUREMENT RESULTS

The LNA under study was fabricated with a standard  $0.25\text{-}\mu\text{m}$  mixed-signal/RF CMOS technology on a p-type

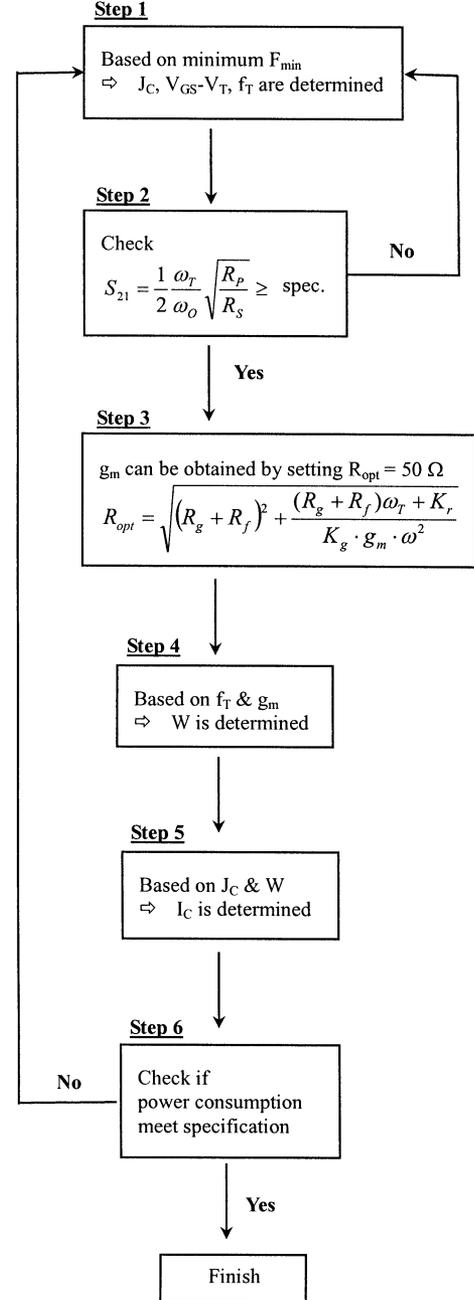


Fig. 6. Flowchart of the design procedures for finding optimized transistor's size and bias.

substrate with substrate resistivity  $R_{\text{sub}} \sim 20 \Omega \cdot \text{cm}$  provided by the commercial foundry United Microelectronics Corporation (UMC), Hsinchu, Taiwan, R.O.C. The main features of the backend processes are as follows. There are five metal layers. Metal-4 (M4) and Metal-5 (M5) were used as the underpass metal layer and the top metal layer of the inductors, respectively. The top metal thickness and underpass metal thickness were 2 and  $0.6 \mu\text{m}$ , respectively. The oxide thickness between top metal and underpass metal, and the oxide thickness between underpass metal and silicon substrate were 1 and  $6.2 \mu\text{m}$ , respectively. No patterned ground shield was implemented below the inductors. Normal substrate thickness was approximately  $750 \mu\text{m}$ . Low- $k$  dielectric material was used

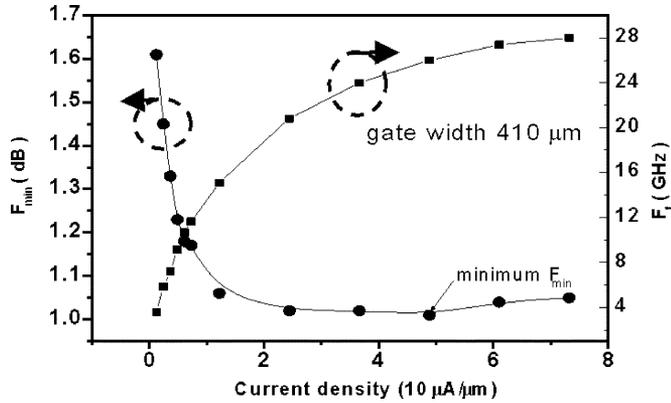


Fig. 7.  $F_{min}$  and  $f_T$  versus current density  $J_C$  of a test device with gatewidth  $410 \mu\text{m}$ .

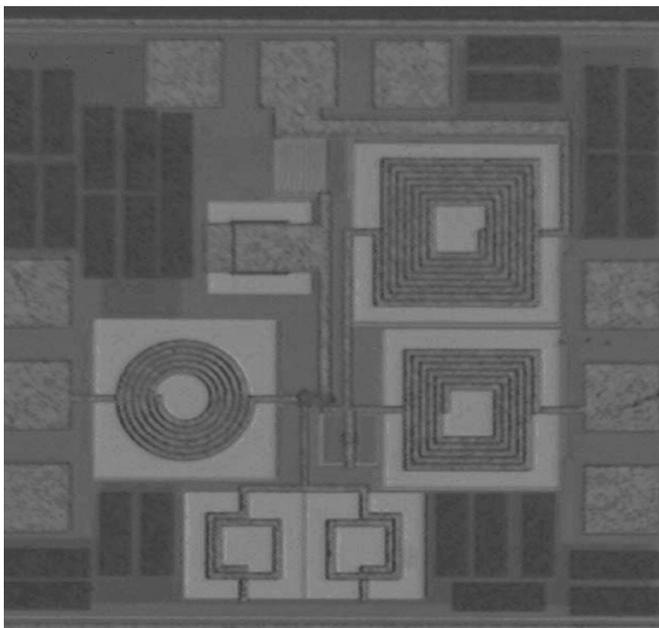


Fig. 8. Die photograph of the LNA.

as the inter-metal-dielectric (IMD) layers for high-performance mixed-signal/RF-CMOS applications.

Fig. 8 presents a die photograph of the LNA. This circuit, which occupies an area of  $500 \times 795 \mu\text{m}^2$ , is operated with  $V_{DD} = 2 \text{ V}$ . The substrate of the LNA was thinned down to approximately  $20 \mu\text{m}$  for the purpose of studying the effect of silicon substrate thickness on the NF performance of the LNA. Fig. 9 shows the detailed process flow to thin down the substrate of the LNA. First, stick the front side (the side with the LNA) of the chip ( $5 \text{ mm} \times 5 \text{ mm}$ ) to the glass substrate with wax. Second, polish the back of the chip mechanically to the target thickness, i.e.,  $20 \mu\text{m}$ , by holding the glass substrate facing down onto a rotating pad with a diamond sand paper. Third, apply photosensitive epoxy to the back of the chips and stick another glass substrate to it, followed by a 3-s UV exposure for epoxy curing and activation. Viscosity is enhanced as the exposure time increases. Fourth, soften the wax by heating so that the glass substrate on the front side of the chip can be removed. Finally, clean the chip by acetone. The thickness of the overall die plus photosensitive epoxy is approximately  $40 \mu\text{m}$ . Since a glass substrate has

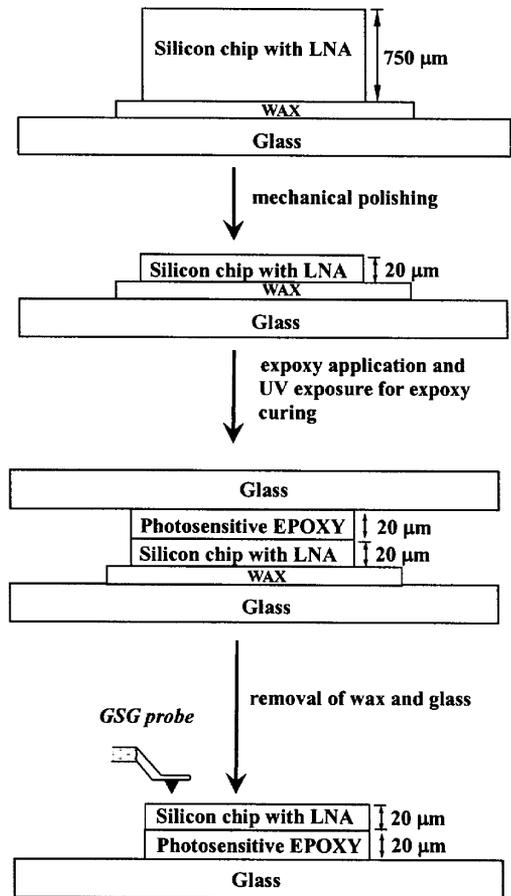


Fig. 9. Detailed process flows of silicon substrate thinning.

been attached to the backside of the chip, it is easy to handle the chip. For the current small  $5 \text{ mm} \times 5 \text{ mm}$  chip, it is found that the yield is 100% in the laboratory. It is not clear to us that if this process will be a low-cost and high-yield process in the industry. However, as technology advances, we believe that the yield of this process should also be high even for large diameter wafers used in the industry.

The noise and scattering parameters were measured on wafer using an automated NP5 measurement system from ATN Microwave Inc., Palo Alto, CA. The measured characteristics of NFs versus frequency for the LNA on a normal substrate with different power consumptions are shown in Fig. 10(a). Minimum NFs of 2.7, 2.9, and 3.3 dB were obtained at the frequency 5.2 GHz with power consumptions of 12, 7.6, and 3.6 mW, respectively. The frequency (5.2 GHz) where minimum NF happens is denoted by  $\omega_{On}$ . Fig. 10(b) compares the measured characteristics of NFs versus frequency for the LNA on both normal and thin substrates with power consumption of 10 mW. Minimum NFs of 2.17 and 3.0 dB are obtained around the frequency  $\omega_{On} = 5.2 \text{ GHz}$  for the LNAs on the thin and normal substrates, respectively. Our results unequivocally demonstrate that low NFs and low power consumptions can be achieved simultaneously with on-chip input and output matching networks in CMOS technology at 5-GHz band. In fact, the difference between minimum and  $50\text{-}\Omega$  NF is only 0.2 dB at 5.2 GHz, indicating an approximation to optimum noise matching due to the design of  $R_{opt}$  to the desired value of  $50 \Omega (= Z_s)$ . From our

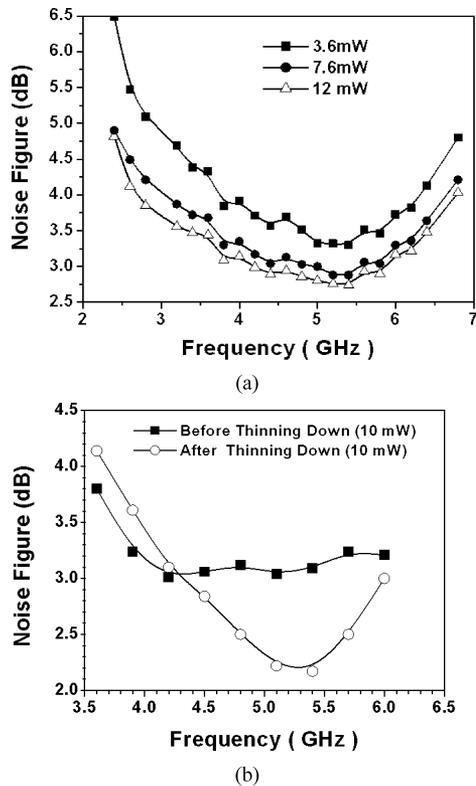


Fig. 10. (a) Measured characteristics of NFs versus frequency for the LNA on a normal substrate ( $750 \mu\text{m}$ ) with different power consumptions. (b) Measured characteristics of NFs versus frequency for the LNA on both normal ( $750 \mu\text{m}$ ) and thin ( $20 \mu\text{m}$ ) substrates with 10-mW power consumption.

experimental data, we conclude that setting  $R_{\text{opt}} = 50 \Omega$  does not necessarily require large  $C_{\text{gs}}$  (device size) or large current, at least for the CMOS process we used.

Fig. 11(a) shows the measured and simulated quality factors versus frequency characteristics of a 5.5-turn testing inductor fabricated at the same time with the LNAs on both normal ( $750 \mu\text{m}$ ) and thin substrates ( $50 \mu\text{m}$  and  $20 \mu\text{m}$ ). The track width and gap between tracks of this inductor were 8 and  $2 \mu\text{m}$ , respectively. The inner dimension inside the inner coil was  $60 \mu\text{m} \times 60 \mu\text{m}$ . As can be seen, the measured maximum quality factors ( $Q_{\text{max}}$ ) were 6.9, 8.5, and 11.3, respectively, for silicon substrate thicknesses of 750, 50, and  $20 \mu\text{m}$ . The measured self-resonance frequencies ( $f_{\text{SR}}$ ) were 13.5, 14.7, and 16.7, respectively, for silicon substrate thicknesses of 750, 50, and  $20 \mu\text{m}$ , i.e., 63.8% (from 6.9 to 11.3) and 23.7% (from 13.5 to 16.7) performance improvements of  $Q_{\text{max}}$  and  $f_{\text{SR}}$ , respectively, are achieved if the silicon substrate is thinned down from 750 to  $20 \mu\text{m}$ . This means the silicon substrate thinning is effective in improving both the quality factor and resonant frequency of the inductors due to the reduction of silicon substrate loss. It is interesting to note that silicon substrate thinning can largely improve both the  $Q_{\text{max}}$  and  $f_{\text{SR}}$  of an inductor, while metal or polysilicon pattern-ground-shield (PGS) can only improve  $Q_{\text{max}}$ , but deteriorate  $f_{\text{SR}}$  of an inductor [26]. Taking the inductor with the best performance (i.e., with polysilicon PGS on a silicon substrate with resistivity  $R_{\text{sub}} \sim 11 \Omega \cdot \text{cm}$ ) in [26], for example, the improvement in  $Q_{\text{max}}$  is only 33% (from

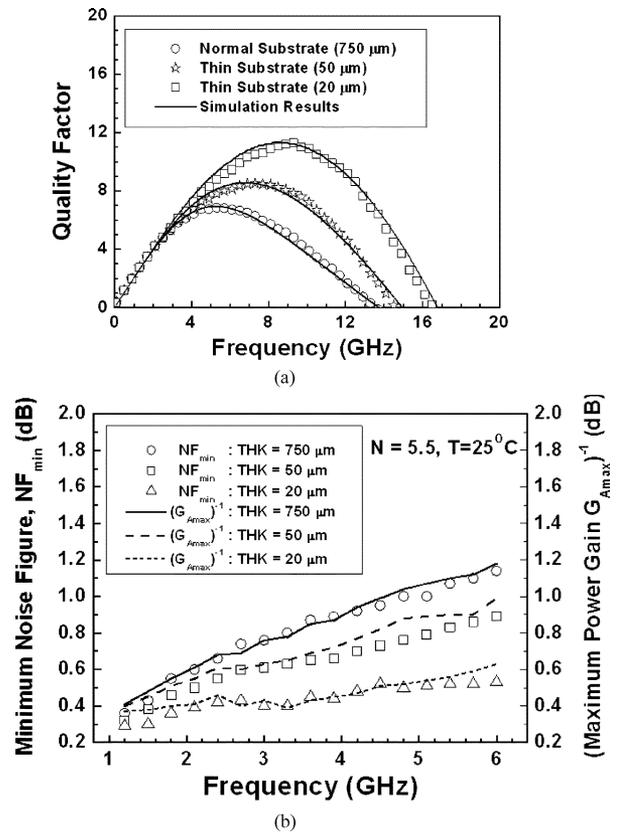


Fig. 11. (a) Measured and simulated quality factors versus frequency characteristics. (b) Measured minimum NFs and the inverse of maximum available power gains versus frequency characteristics of a 5.5-turn testing inductor fabricated at the same time with the LNAs on both normal ( $750 \mu\text{m}$ ) and thin ( $50 \mu\text{m}$  and  $20 \mu\text{m}$ ) substrates.

5.08 to 6.76), but the deterioration in  $f_{\text{SR}}$  is up to  $-47.1\%$  (from 6.8 to 3.6).

The measured  $NF_{\text{min}}$  of a 5.5-turn testing gate inductor was compared to the calculated  $10 \log(1/G_{\text{Am,ax}})$  obtained from the measured  $S$ -parameters at various silicon substrate thicknesses (750, 50, and  $20 \mu\text{m}$ ), as shown in Fig. 11(b). As can be seen, the measured  $NF_{\text{min}}$  conformed well to the calculated  $10 \log(1/G_{\text{Am,ax}})$  [24]. In addition, the measured  $NF_{\text{min}}$  at 5.4 GHz was 1.07, 0.83, and 0.52 dB, respectively, for silicon substrate thicknesses of 750, 50, and  $20 \mu\text{m}$ . This means the silicon substrate thinning is effective in improving  $NF_{\text{min}}$  of the inductors due to the reduction of silicon substrate loss. Besides, the measured  $S$ -parameters of a testing MOSFET with gate length of  $0.25 \mu\text{m}$  fabricated at the same time with the LNAs on both normal ( $750 \mu\text{m}$ ) and thin substrates ( $50 \mu\text{m}$  and  $20 \mu\text{m}$ ) are nearly the same, i.e., silicon substrate thinning shows no effects on the performance of MOSFETs. Based on the above results, the reason why silicon substrate thinning can improve the NF of an LNA can be explained as follows. Since the thickness of the thin substrate ( $\sim 20 \mu\text{m}$ ) is much smaller than the diameter of the inductor (on the order of  $100 \mu\text{m}$ ) [26], [27] and much larger than the gate length of the MOSFETs ( $0.25 \mu\text{m}$ ), the reduction of the NF of an LNA with a thin substrate should be mainly due to the reduction of substrate loss of the inductors in the LNA. The measurement of the NFs on the 5.5-turn testing inductor shows a 0.55-dB reduction of NF

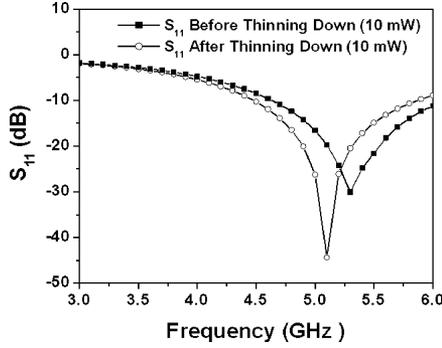


Fig. 12. Measured characteristics of input return loss ( $S_{11}$ ) versus frequency for the LNA on both normal ( $750 \mu\text{m}$ ) and thin ( $20 \mu\text{m}$ ) substrates with 10-mW power consumption.

(from 1.07 to 0.52 dB) after substrate thinning to  $20 \mu\text{m}$  [see Fig. 11(b)]. This result demonstrates the 0.83-dB reduction of the NF of the LNA (from 3.0 to 2.17 dB) is reasonable.

Fig. 12 shows the measured characteristics of  $S_{11}$  versus frequency for the LNAs on both normal and thin substrates with power consumption of 10 mW. Minimum return losses of  $-45$  dB at  $\omega_O$  of 5.1 GHz (thin substrate) and  $-30$  dB at  $\omega_O$  of 5.3 GHz (normal substrate) were achieved as a result of the right choice of  $L_S$ . The in-band ( $5.15 \sim 5.35$  GHz) return losses were below  $-18$  dB and  $-22$  dB for normal and thin substrates, respectively, indicating a very good match even over the band. Note that  $\omega_O$  is very close to  $\omega_{On}$ . This is important for simultaneous input matching and noise matching. In fact, it can be shown from (4) that the frequency  $\omega_{On}$  is given by

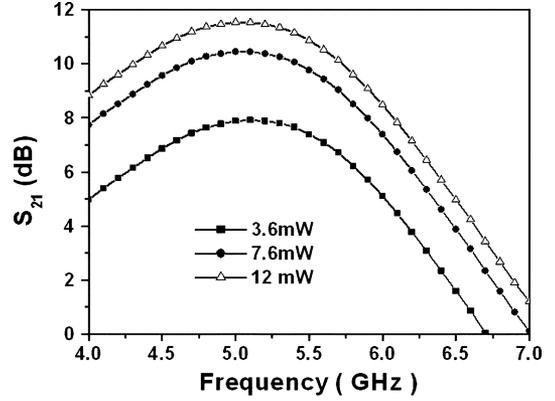
$$\begin{aligned} \omega_{On} &= \omega_O \sqrt{K_C} \sqrt{1 - \frac{\omega_O^2 C_{gs}^2 (R_S + R_g + R_{lg} + R_{fg} + R_f)^2}{2K_C}} \\ &\approx \omega_O \sqrt{K_C} \sqrt{1 - \frac{1}{2Q_S^2 K_C}}. \end{aligned} \quad (23)$$

If  $Q_S^2 \gg 1$  and  $K_C$  is not far from unity, (23) reduces to

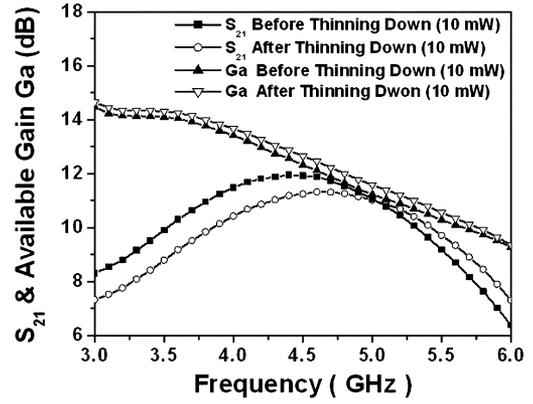
$$\left( \frac{\omega_{On}}{\omega_O} \right)^2 = K_C. \quad (24)$$

Take, for example, the experimental values of the LNA on a normal substrate at power consumption of 10 mW, i.e.,  $\omega_{On} = 5.2$  GHz and  $\omega_O = 5.3$  GHz, as shown in Figs. 10(b) and 12, respectively. A value of  $K_C = 0.96$  was determined, which is close to 1. The fact that  $K_C$  approximates 1 explains why  $\omega_O$  and  $\omega_{On}$  are so close to each other. Thus,  $K_C$  can be interpreted physically as a measure of the separation between  $\omega_O$  and  $\omega_{On}$ . In other words, if a CMOS process does not result in a  $K_C$  close to 1, it is almost hopeless for circuit designers to design a circuit with simultaneous input impedance matching and noise matching over the narrow band of interest.

The measured transducer gain ( $S_{21}$ ) for the LNA on a normal substrate with different power consumptions is shown in Fig. 13(a). The bandpass nature of this amplifier is evident from the plot. Under the bias condition of 12 mW, the gain has



(a)



(b)

Fig. 13. Measured transducer gain ( $S_{21}$ ) versus frequency of the LNA: (a) on a normal substrate ( $750 \mu\text{m}$ ) with different power consumptions and (b) on both normal ( $750 \mu\text{m}$ ) and thin ( $20 \mu\text{m}$ ) substrates with 10-mW power consumption.

a peak value of 11.5 dB. For a direction conversion receiver, the load resistance is not necessarily  $50 \Omega$  and a higher gain can be expected. For lower power consumptions, the characteristics are similar, but with lower gains of 10.4 dB at 7.6 mW and 8 dB at 3.6 mW. One figure-of-merit is the ratio of gain to dc power consumption [2]. The values of gain to dc power consumption attained by this CMOS LNA were 0.95, 1.4, and 2.2 dB/mW at three different power consumptions of 12, 7.6 and 3.6 mW, respectively. The measured  $S_{21}$  and available gain for the LNA on both normal and thin substrates with power consumption of 10 mW are shown in Fig. 13(b). The available gain has peak values of 10.9 and 11.2 dB for normal and thin substrates, respectively. The values of gain to dc power consumption attained are 1.12 (thin substrate) and 1.09 (normal substrate) dB/mW. As can be seen clearly in Table I, the obtained ratios of gain to dc power consumption are comparable to the other state-of-the-art  $C$ -band LNAs shown in Table I.

Microwave power performances were measured by a load-pull ATN system with automatic tuners. The measured  $P_{1 \text{ dB}}$  and input IP3 data for the LNA on a thin ( $20 \mu\text{m}$ ) substrate under power consumption of 10 mW are shown in Fig. 14. As can be seen, an input  $P_{1 \text{ dB}}$  of  $-8.3$  dBm and an input IP3 of 0.3 dBm were obtained. Other measured  $P_{1 \text{ dB}}$  and input IP3 data are summarized in Table I. A summary of the measured amplifier characteristics at different bias conditions is also included in Table I.

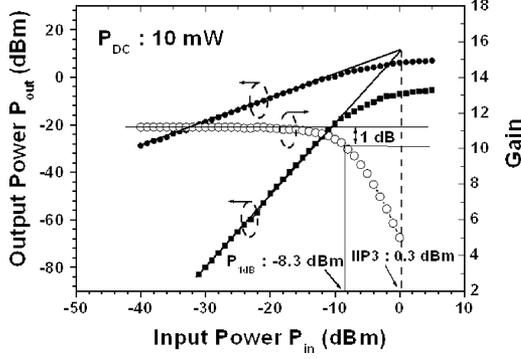


Fig. 14. Measured input  $P_{1\text{ dB}}$  and input IP3 for the LNA on a thin substrate ( $20\ \mu\text{m}$ ) with 10-mW power consumption.

#### IV. CONCLUSIONS

A method of designing  $R_{\text{opt}}$  to a desired value by the selection of transistor device size and transconductance or bias is proposed. By setting  $R_{\text{opt}} \sim 50\ \Omega$ , NFs of 2.17 and 3.0 dB, and input return losses of  $-45$  and  $-30$  dB at the 5-GHz band from a monolithic CMOS LNA with 10-mW dissipation on both thin ( $\sim 20\ \mu\text{m}$ ) and normal ( $750\ \mu\text{m}$ ) substrates are demonstrated with a standard  $0.25\text{-}\mu\text{m}$  CMOS process provided by a commercial foundry. The fact that  $K_c$  is close to 1 in the CMOS process we used can achieve low NF and low input return loss simultaneously in the narrow band of interest. In addition, substrate thinning is effective in reducing the NF. The result also unequivocally demonstrates that low NFs and low power consumption can be achieved simultaneously with on-chip input and output matching networks in CMOS technology at the 5-GHz band. From both a performance and a cost perspective, these experimental results show that CMOS is very competitive with silicon bipolar and GaAs technologies.

#### APPENDIX

##### DERIVATION OF THE NF FOR AN FET WITH GATE AND SOURCE INDUCTORS

A noise analysis of the circuit shown in Fig. 1(b) quantifies the effects of the gate and source inductors. An equivalent circuit for noise calculation is depicted in Fig. 1(b). By definition the NF,  $F$  can be expressed in the form

$$F = \frac{\overline{i_{n,\text{out}}^2}}{\overline{i_{s,o}^2}} = 1 + \frac{\overline{|i_{rgo} + i_{lgo} + i_{go} + i_{rfo} + i_{lfo} + i_{do}|^2}}{\overline{i_{s,o}^2}} \quad (25)$$

where  $i_{n,\text{out}}$  stands for the total noise current in the short-circuited drain-source path originated from the noise current components  $i_{rgo}$ ,  $i_{lgo}$ ,  $i_{go}$ ,  $i_{rfo}$ ,  $i_{lfo}$ ,  $i_{do}$ , and  $i_{so}$  produced by the

noise generators from transistor gate resistance noise  $e_{rg}$ , series resistance of gate inductor  $e_{lg}$ , induced gate noise current  $i_g$ , transistor source resistance noise  $e_{rf}$ , series resistance of source inductor  $e_{lf}$ , drain noise current  $i_d$ , and signal source resistance noise  $e_s$ . The noise generators representing the extrinsic thermal sources are given by their mean square values  $\overline{|e_{rg}^2|} = 4kTR_g\Delta f$ ,  $\overline{|e_{lg}^2|} = 4kTR_{lg}\Delta f$ ,  $\overline{|e_{rf}^2|} = 4kTR_f\Delta f$ ,  $\overline{|e_{lf}^2|} = 4kTR_{lf}\Delta f$ , and  $\overline{|e_s^2|} = 4kTR_S\Delta f$ . A careful analysis yields the following equations:

$$i_{rgo} = e_{rg} \frac{\frac{g_m}{j\omega C_{gs}}}{\frac{1}{j\omega C_{gs}} + \frac{g_m L_s}{C_{gs}} + Z_t} \quad (26)$$

$$i_{lgo} = e_{lg} \frac{\frac{g_m}{j\omega C_{gs}}}{\frac{1}{j\omega C_{gs}} + \frac{g_m L_s}{C_{gs}} + Z_t} \quad (27)$$

$$i_{rfo} = e_{rf} \frac{\frac{g_m}{j\omega C_{gs}}}{\frac{1}{j\omega C_{gs}} + \frac{g_m L_s}{C_{gs}} + Z_t} \quad (28)$$

$$i_{lfo} = e_{lf} \frac{\frac{g_m}{j\omega C_{gs}}}{\frac{1}{j\omega C_{gs}} + \frac{g_m L_s}{C_{gs}} + Z_t} \quad (29)$$

$$i_{so} = e_s \frac{\frac{g_m}{j\omega C_{gs}}}{\frac{1}{j\omega C_{gs}} + \frac{g_m L_s}{C_{gs}} + Z_t} \quad (30)$$

$$i_{go} = i_g \frac{\frac{g_m}{j\omega C_{gs}} Z_t}{\frac{1}{j\omega C_{gs}} + \frac{g_m L_s}{C_{gs}} + Z_t} \quad (31)$$

$$i_{do} = i_d \frac{Z_t + \frac{1}{j\omega C_{gs}}}{\frac{1}{j\omega C_{gs}} + \frac{g_m L_s}{C_{gs}} + Z_t} \quad (32)$$

Inserting (26)–(32) into (25) yields

$$F = 1 + \frac{R_g + R_{lg} + R_{lf} + R_f}{R_S} + \frac{1}{4kTR_S\Delta f} \left| Z_t i_g + \frac{1 + j\omega C_{gs} Z_t}{g_m} i_d \right|^2 \quad (33)$$

Substituting  $Z_t = Z_S + R_g + R_f + R_{lg} + R_{lf} + j\omega(L_g + L_s)$  into (33), we get (34), shown at the bottom of this page. By

$$F = 1 + \frac{R_g + R_{lg} + R_{lf} + R_f}{R_S} + \frac{1}{4kTR_S\Delta f} \left| i_g + \frac{j\omega C_{gs}}{g_m} i_d \right|^2 \left| Z_S + R_g + R_{lg} + R_{lf} + R_f + j\omega(L_g + L_s) + \frac{i_d}{g_m \left( i_g + \frac{j\omega C_{gs}}{g_m} i_d \right)} \right|^2 \quad (34)$$

analogy with the results derived by Pucel *et al.*, (34) can be put in the form of (4) if  $G_n$ ,  $R_u$ , and  $Z_C$  are defined as follows:

$$G_n = \left| \frac{j\omega C_{gs}}{g_m} \sqrt{g_m P} - jC \sqrt{R \frac{\omega^2 C_{gs}^2}{g_m}} \right|^2 + (1 - C^2) R \frac{\omega^2 C_{gs}^2}{g_m} \quad (35)$$

$$R_u = R_g + R_{\ell g} + R_{\ell f} + R_f + \frac{P}{g_m} \frac{(1 - C^2)}{G_n} R \frac{\omega^2 C_{gs}^2}{g_m} \quad (36)$$

$$Z_C = R_g + R_{\ell g} + R_{\ell f} + R_f + j\omega(L_g + L_S) + \frac{1}{G_n} \left( \frac{-Pj\omega C_{gs}}{g_m} + \frac{jC \sqrt{PR\omega^2 C_{gs}^2}}{g_m} \right) \quad (37)$$

and, thus, the NF of an FET with gate and source inductors are derived.

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