almost no effect on the value of $\eta$ : the difference between the $\eta$-values for a patch (broken curve) and a dipole (dotted curve) is less than 0.02 for $\varepsilon_{r}=2 \cdot 55$, and nearly zero for $\varepsilon_{r}=12 \cdot 8$. As we are only interested in resonant antennas, the length $L$ of the patch is not of importance: it is determined by $W, h, \varepsilon_{r}$ and the resonant frequency. Therefore only two parameters are needed to describe the space wave efficiency: $\varepsilon_{r}$ and $h / i_{0}$. A first estimate of $\eta$ uses a linear $h / i_{0}$ dependence:

$$
\begin{equation*}
\eta=10-\sqrt{ }\left(\varepsilon_{r}-1\right)\left(\frac{h}{\lambda_{0}}\right) \times 3.4 \tag{2}
\end{equation*}
$$

The factor $\sqrt{ }\left(\varepsilon_{r}-1\right)$ in the second term assures that $\eta=1$ for an air dielectric, and that $\eta$ decreases faster with increasing $h / i_{0}$ as $\varepsilon_{r}$ increases. Eqn. 2 can also be written in terms of the cutoff frequency of the first-order TE mode:

with $f_{c 1}=c_{0} /\left[4 h \sqrt{ }\left(\varepsilon_{r}-1\right)\right]$.

Fig. 5 Space wave efficiency for wide patch antenna on substrate with $\varepsilon_{r}=4.0$

$$
--- \text { patch }^{5} \quad \text { eqn. } 4
$$

From Figs. 2 and 3, we see that the linear dependence works well for small $h / \lambda_{0}$ (until $0 \cdot 06$ ), but that for larger substrate thicknesses and small $\varepsilon_{r}$ some extra terms are needed. (For $\varepsilon_{r}=12.8$ the linear curve is extended practically to the point where the $\mathrm{TE}_{1}$ mode can propagate.) The final expression for $\eta$ is

$$
\begin{equation*}
\eta=1 \cdot 0-3 \cdot 4 H+\frac{1600}{\varepsilon_{r}^{3}}\left(H^{3}-100 H^{5.6}\right) \tag{4}
\end{equation*}
$$

with $H=\sqrt{ }\left(\varepsilon_{r}-1\right)\left(h / \lambda_{0}\right)=0 \cdot 25\left(f / f_{c 1}\right)$.
In Figs. 2-6, the solid curve represents the results obtained with eqn. 4. As one can see, there is excellent agreement with the data from the Green function methods.

Range of validity: For practical purposes, it is largely sufficient if $\eta$ can be calculated for $f<0 \cdot 8 f_{\mathrm{c} 1}$, which is equivalent to $H<0.20$. For $\varepsilon_{r}=2.55$ this corresponds to $h / \lambda_{0}=0.16$, and for $\varepsilon_{r}=12.8$ to $h / \lambda_{0}=0.058$. For this range of $H$ a maximal


Fig. 6 Space wave efficiency for wide and narrow patch antenna on substrate with $\varepsilon_{r}=9.8$
--- patch $^{5} \ldots \ldots$. dipole $^{5}-$ eqn. 4
difference of 0.04 is found between eqn. 4 and Pozar's results ${ }^{1}$ for a patch $0.3 i_{0}$ wide (Figs. 2 and 3). A similarly small deviation of 0.05 is found between eqn. 4 and Perlmutter's ${ }^{5}$ results (Figs. 4, 5 and 6). As the difference between $\eta$ for dipoles and patches is always less than 0.02 , eqn. 4 also holds for dipoles.

Conclusion: A very simple expression is presented that summarises the available data for space wave efficiency of rectangular microstrip antennas. Its arguments are $\varepsilon_{r}$ and $h / \lambda_{0}$. The expression is valid for dipoles and patches, and has been checked against numerical data for $\varepsilon_{r}=2 \cdot 2,2 \cdot 55,4,9.8$ and $12 \cdot 8$. The maximal difference between numerical data and the closed-form expression is 0.05 for $\sqrt{ }\left(\varepsilon_{r}-1\right)\left(h / \lambda_{0}\right)<0.20$.
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## PERFORMANCE ANALYSIS OF HIGH-DENSITY WDM SYSTEMS USING RAMAN AMPLIFICATION

Indexing terms: Optical communications, Optical fibres, Nonlinear optics, Multiplexing

The applications of Raman amplifiers as repeater amplifiers or post-transmitter amplifiers in a high-density WDM system are theoretically investigated. There exists an optimum pump power which results in maximum amplifier gain. The result shows that amplifier gains up to 50 dB and 20 dB are achievable for use as a repeater and a post-transmitter amplifier, respectively.

Introduction: High-density, wavelength-division-multiplexed (HDWDM) systems provide a means for exploiting the vast bandwidth of a single-mode fibre. ${ }^{1}$ One of the limitations imposed on an HDWDM system is the power depletion caused by stimulated Raman scattering (SRS), ${ }^{2.3}$ so that both the number of channels and transmission power are limited. On the other hand, SRS can be used to optically amplify multichannel signals with single pump power, ${ }^{4}$ which is of special interest in an HDWDM system. The fibre Raman amplifier can be either used as a repeater amplifier to boost weak signals, or used at the transmitting end to amplify the multichannel signals so as to increase system transmission distance and relax the limitation caused by SRS. This letter investigates the application of Raman amplification in an HDWDM system.

Analysis: The nonlinear pumping process in an HDWDM system is complicated and depends on channel spacing, number of channels, as well as the pump and signal powers. Here we analyse the signals of an $N$-channel HDWDM fibre transmission system with Raman amplification, and consider the case that all signals are pulse-modulated while the pump is a continuous wave.

Let $A$ and $\alpha$ denote the effective cross-section and loss coefficient of the fibre, respectively. To simplify the analysis, we assume that the Raman gain has a Lorentzian lineshape, while the actual lineshape in fibres is much more complicated. ${ }^{5}$ The lineshape is given as

$$
\begin{equation*}
g\left(v_{R}\right)=\frac{g_{0}(w / 2)^{2}}{\left(v_{R}-v_{0}\right)^{2}+(w / 2)^{2}} \tag{1}
\end{equation*}
$$

where $g_{0}$ is the peak Raman gain coefficient, $w$ the full width at half-maximum of the Lorentzian lineshape, $v_{R}$ the Raman shift between the two coupling waves, and $v_{0}$ the Raman shift corresponding to the peak gain.

Let $v_{p}$ and $v_{s i}$ denote the lightwave frequencies of the pump and the $i$ th signal in the HDWDM system. In an HDWDM system the linewidths of the signals are much smaller than $w$, and hence the Raman gain for the signals is assumed to be constant. The Raman gain constant coupling the pump and the $i$ th signal, $g_{i}$, and the gain constant coupling the $i$ th and $j$ th signal channels, $g_{i j}$, can then be calculated from eqn. 1 with appropriate $v_{R}$.

Let $L$ denote the transmission distance. The signal power $S_{i}(0), i=1,2, \ldots, N$, and the pump power $P(0)$ are injected at $z=0$ and travel in the $+z$ direction. The differential equations governing the signals and the pump propagation are given by

$$
\begin{align*}
\frac{d S_{i}(z)}{d z}= & {\left[-\alpha_{s}+\frac{g_{i}}{A} P_{1}(z)+\sum_{j=1}^{i-1} \frac{g_{i j} S_{j}(z)}{A}\right.} \\
& \left.-\sum_{m=i+1}^{N} \frac{v_{s i}}{v_{s m}} \frac{g_{i m} S_{m}(z)}{A}\right] S_{i}(z) \quad i=1,2, \ldots, N  \tag{2}\\
\frac{d P(z)}{d z}= & -\left[\alpha_{p}+\sum_{i=1}^{N} \frac{g_{i} v_{p}}{A v_{s i}} S_{i}(z)\right] P(z) \tag{3}
\end{align*}
$$

Here we assume $v_{s 1}>v_{s 2} \ldots>v_{s N}$ and that the $N$ channels are equally spaced with channel spacing $\Delta v$. The second term in eqn. 2 denotes the coupling between the $i$ th signal and the pump; the third and the last terms express the crosscoupling among the signal channels. Because of the crosscoupling among the signal channels, the optical power of the shorterwavelength channels will be depleted by the longerwavelength channels, and will be most severe for the shortest-wavelength channel (channel 1). As a result, the system transmission distance will be limited by the achievable amplifier gain of channel 1. Numerical calculation is carried out to estimate the achievable amplifier gain. We consider the worst case that all the channels are in the 'on' state, in which channel 1 is most depleted. For simplicity we choose an odd number of channels, and locate the middle channel at the centre of the Raman gain profile. The amplifier gain of channel 1 at $z=L$ is defined as

$$
\begin{equation*}
G=10 \log \frac{S_{1}(L)}{S_{1}(0) e^{-x L}} \tag{4}
\end{equation*}
$$

where $S_{1}(L)$ is the power of channel 1 at $z=L$ with Raman amplification.

The relationship between the gain of channel 1 and the pump power is shown in Fig. 1. Here two regions can be characterised. One is the linear region in which $G$ increases linearly with $P(0)$, while the other is the saturation region where $G$ gradually reaches a maximum value and decreases as $P(0)$ further increases. For use as post-transmitter amplifiers $\left(S_{i}(0)=0.1 \mathrm{~mW}\right)$, the achievable gain is much smaller and the maximum gain occurs at a lower pump power level than those used as repeater amplifiers $\left(S_{i}(0)=0 \cdot 1 \mu \mathrm{~W}\right)$. The influence of channel number $N$ on $G$ is shown in Fig. 2, where $g_{1}$ and the
total signal span ( $N-1$ ) $\Delta v$ are kept constant. The degradation of $G$ as $N$ increases is expected since more power of channel 1 is depleted. When used as repeater amplifiers, $G$ is insensitive to the channel number $N$ in the linear region but degrades in the saturation region. In the linear region, because channel 1 obtains much more power from the pump than that depleted by the other channels, $G$ is nearly independent of $N$.


Fig. $1 G$ as function of pump power for $N=H$
Solid lines (post-transmitter amplifiers): $S_{i}(0)=0.1 \mathrm{~mW}$; broken lines (repeaters): $S_{i}(0)=0.1 \mu \mathrm{~W}$. For convenience we use wavelength unit for $\Delta v . g_{0}=7.5 \times 10^{-14} \mathrm{~m} / \mathrm{W}, A=5 \times 10^{-11} \mathrm{~m}^{2}$, $\alpha=0.2 \mathrm{~dB} / \mathrm{km}, W=240 \mathrm{~cm}^{-1}, v_{0}=460 \mathrm{~cm}^{-1}, L=150 \mathrm{~km}$

However, in the saturation region the depletion by the other channels becomes comparable to that obtained from the pump, and thus degradation results. Since it is essentially operating in the saturation region when used as a posttransmitter amplifier, $G$ degrades as $N$ increases. When the pump power increases, the signal power of channel 1 depleted by the other channels may exceed that obtained from the pump, so that the gain decreases. Therefore there exists an optimum pump power which results in maximum gain of channel 1. As shown in the Figures, for use as a repeater amplifier, an amplifier gain up to 50 dB is achievable, which corresponds to 250 km repeater spacing for $0.2 \mathrm{~dB} / \mathrm{km}$ fibre loss. For use as a post-transmitter amplifier, more than 20 dB gain is still obtainable, corresponding to 100 km extended transmission length, and the constraint imposed by Raman crosstalk is relaxed because the depleted power of channel 1 by the other channels is compensated by the pump.


Fig. 2 Effect of channel number on $G$
Solid lines (post-transmitter amplifiers): $S_{i}(0)=0.1 \mathrm{~mW}$; broken lines (repeaters): $S_{i}(0)=0.1 \mu \mathrm{~W}$. Same parameters used as in Fig. 1; $(N-1) \Delta v=40 \mathrm{~nm}$

Conclusions: We have investigated the properties of Raman amplification in an HDWDM system. The results show that there exists an optimum pump power to yield a maximum amplifier gain. A high gain is achievable for use as a repeater amplifier, and a modest gain is obtainable when used as a post-transmitter amplifier. Based on these results, we conclude
that Raman amplifiers are potential candidates to amplify multichannel signals in an HDWDM system.
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## FEMTOJOULE BISTABLE OPTICAL

 SWITCHING OF INHOMOGENEOUSLY PUMPED LASER DIODE AT 500 MHz USING MODE-LOCKED TUNABLE DIODE LASER
## Indexing terms: Semiconductor lasers, Optical switching, Non-

 linear opticsWe have investigated the nonlinear transfer characteristics and temporal response of bistable three-section lasers within a broad wavelength interval ( 30 nm ), when switched with picosecond optical pulses ( 20 ps ) at a high repetition rate. The minimum input coupled switch-on energy was 0.7 fJ . The shortest switching time was 60 ps .

In this letter we present results comparable to the lowest switching energies, ${ }^{1}$ and at the same time the highest repetition rates ${ }^{2}$ reported for bistable optical devices.

Experiment: The bistable laser diode (BLD) was a threesection GaInAsP diode, with a lasing wavelength of 1310 nm . The absorber section was situated at the facet where the optical switching pulses were incident. The bias currents were chosen so that the BLD was kept 0.1 mA below the electrical switch-on threshold. Further details can be found in Reference 3.

We measured the photocurrent generated in the BLD when it was reverse biased to optimise and evaluate the input coupling efficiency, which was approximately $10 \%$. A pinhole transmission measurement of the input spot size was in very good agreement with this input coupling efficiency.

A mode-locked diode laser was employed for switching the BLD. The mode-locked laser produced optical pulses of $20-$ 40 ps FWHM, as measured by autocorrelation. These pulses were monitored on a sampling oscilloscope by using a pin photodiode with a rise time of 60 ps . The wavelength of the mode-locked laser was controlled by a Fabry-Perot étalon placed in an external cavity. The spectral width of the pulses was $\leq 3 \AA$ for wavelengths less than 1300 nm and $\leq 5 \AA$ for longer wavelengths.

To achieve fast switch-off 1 ns after the set-pulse, a short negative electrical pulse was employed to extract the charge carriers from the absorber section. ${ }^{2}$ The pulse amplitude was around 20 mA and the pulse width was less than 130 ps (FWHM).

Minimum switching energy: We measured the minimum input energy for switching $E_{\text {min }}$ in front of the microscope objective
for input coupling ( $\mathrm{NA}=0.83$ ). The output energy $E_{\text {output }}$ when switching with minimum input energy, was measured after the microscope objective for output coupling ( $\mathrm{NA}=0 \cdot 25$ ). The results are plotted against input wavelength in Fig. 1. We found the smallest $E_{\text {min }}$ to be $7 \cdot 2$ fJ, i.e. the input coupled energy was approximately 0.7 fJ , at an input wavelength of 1305.8 nm . This corresponds to less than 5000 input coupled photons. Another feature of the switching characteristics at 1305.8 nm is the high output energy 170 fJ . This optimum wavelength was 4 nm shorter than the main lasing mode of the BLD. We recorded the input and output spectra using a monochromator with a resolution better than $1 \AA$. There were three common features of all the output spectra obtained: (a) the attenuated transmitted input signal, $(b)$ an initial lasing BLD-mode positioned quite near the input wavelength of $(a)$, and $(c)$ a broad dominating laser spectrum of the BLD which was centred at 1310 nm . This implies that the BLD reaches the steady-state within 1 ns .


Fig. 1 Minimum switching energy $E_{\text {min }}$ plotted against input wavelength Output energy $E_{\text {output }}$ corresponds to input energy $E_{\text {min }}$

We investigated resonance effects by increasing the number of sampled input wavelengths within the interval for optimum switching energy. This was accomplished by temperaturetuning the mode-locked laser. The BLD was switched at several input wavelengths in the interval $1304 \cdot 8-1306 \cdot 1 \mathrm{~nm}$ and with a spectral width of the mode-locked laser pulse of around $1.5 \AA$ (FWHM). This was plotted with $E_{\text {min }}$ and $E_{\text {output }}$ against input wavelength, as in Fig. 1. The investigated interval was larger than the spacing of two internal cavity modes of the BLD. The wavelength difference of the reflected input pulse and the output pulse was simultaneously measured via a beam splitter placed between the mode-locked laser and the BLD. We found no clear resonant behaviour in this interval.

Transfer function: In Fig. 2, we have plotted $E_{\text {output }}$ against $E_{\text {input }}$ for three different input wavelength intervals. The five points in the Figures are the mean values, within each of the three intervals, obtained for $E_{\text {input }}$ equal to $0, E_{\text {min }} / 2, E_{\text {min }}$, $2 E_{\text {min }}$ and $4 E_{\text {min }}$, respectively. To obtain a measure of the spread of results within different input wavelength intervals, we calculated the standard deviations, which were plotted as error bars for $E_{\text {output }}$ and $E_{\text {min }}$ and $E_{\text {min }}$ at each point. The nonlinear shape of the transfer characteristics is more pronounced for the optimum wavelength interval than for long wavelengths, as in Figs. $2 b$ and $c$. The threshold behaviour observed in all three intervals confirms that we have true bistable switching at 500 MHz . Although the set-up was not optimised for output coupling, the maximum pulse energy gain was 14 dB .

Bistable switching time: The shortest deconvolved rise time of the BLD signal was approximately 60 ps when switching in the optimum wavelength interval with a high input energy. The BLD signal rises immediately after the input signal. The input coupled energy could be decreased to 29 fJ without increasing the switching time. The maximum delay time was 0.7 ns , limited by the electrical reset 1 ns after the input pulse.

Summary: We have characterised bistable switching of a threesection bistable laser diode in an input wavelength interval of 30 nm and at a repetition rate of 500 MHz . Bistable switching was performed with less than 5000 input coupled photons. The shortest recorded bistable switching time was approximately 60 ps .

