

# Novel Temperature Characteristics of Gain Behaviors in Quantum-Dot Lasers

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**Abstract** In quantum dots, the increment of temperature results in red shift of gain spectrum. Thermal state-filling and electron-phonon scattering lead to extremely large and even negative  $T_0$ . Theoretical prediction is confirmed experimentally.

## I. INTRODUCTION

Quantum dot is noted for the low threshold current, high differential gain and high characteristics temperature which are good for applications. [1]

## II. DEPENDENCE OF GAIN SPECTRUM ON TEMPERATURE

There are three main causes of dependence of peak wavelength on quantum dot (QD) laser diodes: thermal expansion, thermal state-filling, and non-equilibrium scattering. First, thermal expansion results in decrease of bandgap energy and red shift. The general expression for bandgap dependence around room temperature with small deviation is given by:

$$E_g(T) = E_{g0} - \frac{\alpha T^2}{T + \beta} \dots (1)$$

where the numerical values for InAs are given by [2].

Second, thermal state-filling causes blue shift. More thermal energy provides higher probability for electrons reside in higher energy levels. The last, non-equilibrium scattering results in blue shift of the spectrum of lower quantized states. In quantum dots, transition of strongly-localized electrons involved with phonon can let electrons relax to lower quantized states. With higher temperature, such electron-phonon scattering can increase the carrier density of lower quantized states and cause blue shifts of them, in the meanwhile, decrease the carrier density of higher quantized states and cause red shifts of them.

## III. SCATTERING DEPENDENT ON TEMPERATURE

The capture and relaxation time are determined by electron-phonon scattering with rates as follows:

$$\frac{1}{\tau} = \frac{2\pi}{\hbar} \int |M_{ij}^{if}|^2 (N_q + 1) \delta(E_{ij} - \hbar\omega_q) d^3q \dots (2)$$

However, the dependence of scattering rates can be expressed in power series in positive powers. Consider operation around room temperature with slight variance of temperature, we can

approximate the scattering rates are inversely proportional to T. [4]

## IV. NON-EQUILIBRIUM FERMI-DIRAC DISTRIBUTION

When the carrier capture and relaxation is limited in QD, the distribution of electrons which doesn't follow Fermi-Dirac distribution is given by: [3]

$$f(E_i) = \frac{1}{1 + R \exp\left(\frac{E_i - E_f}{k_B T}\right)}$$

$$\text{where } R = \tau_{c,r} \left( \frac{1}{\tau_e} + \frac{1}{\tau_s} \right) < 1 \dots (3)$$

where  $\tau_{c,r}$  is overall capture/relaxation lifetime, into/in QD,  $\tau_e$  is stimulated emission lifetime out of QD, and  $\tau_s$  is carrier recombination lifetime. The factor  $R < 1$  shows that the phonon bottleneck can lift the Fermi level and increase the probability for electrons in higher energy levels. The gain is given by:

$$g(\hbar\omega) = \frac{2N_D}{W} \int \sigma_g(\hbar\omega, E_i) g_{inh}(E_i) [2f(E_i) - 1] dE_i \dots (4)$$

With small deviation in temperature, the dependence of  $\tau_e$  and  $\tau_c$  can be approximated as linear with T and  $\tau_s$  as a constant. So the shift of quasi-Fermi level is given by

$$\Delta E_f(\Delta T) = \Delta E_g - k_B T \ln(1 - c\Delta T) \dots (5)$$

On the right hand of the equation, with  $\Delta T > 0$  the first term is negative and the second is positive. At certain temperature, we can find either blue or red shift will happen at certain photon wavelength.

In Fig 1, theoretical calculations are performed by assuming a QD carrier density of  $5 \times 10^{12} \text{ cm}^{-2}$  in injector-well structure layer. We can find the peak gain and peak photon energy decrease with increment of temperature. The thermal expansion of the lattice dominates the thermal band-filling effect and the scattering of phonons and electrons from higher energy levels. We find red shift finally. The peak gain decreases with increment of temperature because of lattice expansion.

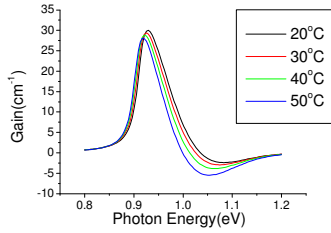


Fig 1. Theoretical Calculation of Gain for 1<sup>st</sup> Quantized State Only

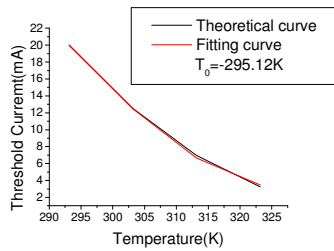


Fig 2. Theoretical Calculation of Threshold Current

In Fig 2., we can find  $T_0 < 0$  for photon energy smaller than the peak photon energy. For ground state  $T_0$  around the peak photon energy approximate infinitely large and even negative such as  $-295.12K$  at photon energy  $0.9 eV$ .

### V. EXPERIMENTAL RESULTS

In Fig 3, red shift with increasing temperature is observed as predicted by the simulation. The 1<sup>st</sup> and 2<sup>nd</sup> quantized states lase at photon energy  $0.98eV$  and  $1.1 eV$  respectively.

In Fig 4., we can find the threshold current decrease with increment of temperature at the photon energy  $0.973 eV$ . Negative temperature effect is observed with different positive and even negative  $T_0$  values at different temperatures.

### VI. CONCLUSION

In quantum dot, the increment of temperature results in red shift by thermal expansion which dominates the blue shift by thermal band-filling and electron-phonon scattering. The latter two causes bring about improved temperature characteristics with extremely large positive  $T_0$  and even negative  $T_0$  around the peak photon energy theoretically and experimentally.

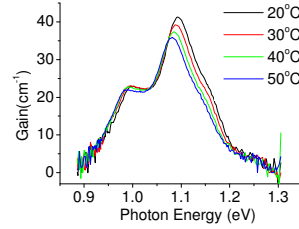


Fig 3. Experimental Gain curves

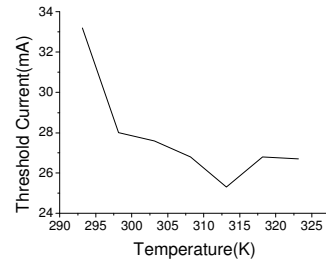


Fig 4. Experimental Threshold Current

### ACKNOWLEDGEMENT

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