

# A combined-cycle refrigeration system using ejector-cooling cycle as the bottom cycle

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## Abstract

A combined-cycle refrigeration system (CCRS) that comprises a conventional refrigeration and air-conditioning system using mechanical compressor (RAC/MC) and an ejector-cooling cycle (EJC) is proposed and studied. The EJC is driven by the waste heat from the RAC/MC and acts as the bottom cycle of the RAC/MC. A system analysis shows that the COP of a CCRS is significantly higher than a single-stage refrigeration system. Improvement in COP can be as high as 18.4% for evaporating temperature of the RAC/MC  $T_e$  at  $-5^\circ\text{C}$ . A prototype of the CCRS was built and tested in the present study. Experimental results show that at  $T_e = -4.5^\circ\text{C}$ , COP is improved by 14% for a CCRS. For  $T_e$  at  $5^\circ\text{C}$ , COP can be improved by 24% for a CCRS with higher condensing temperature of the RAC/MC. The present study shows that the CCRS using the ejector-cooling cycle as the bottom cycle of the RAC/MC is viable. Further improvement in COP is possible since the prototype is not designed and operated at an optimal condition. © 2001 Elsevier Science Ltd and IIR. All rights reserved.

*Keywords:* Refrigerating system; Compression system; Ejection system; Combined system; Subcooling; Design; Performance

## Cycle frigorifiques mixte utilisant un système de refroidissement à éjection

### Résumé

*Les auteurs présentent et étudient un cycle frigorifique mixte (CCRS) comprenant un système frigorifique et de conditionnement d'air classique utilisant un compresseur mécanique (RAC/MC) et un système de refroidissement à éjection (EJC). L'EJC est entraîné par la chaleur récupérée du RAC/MC et sert de cycle d'appui du RAC/MC. Une analyse montre que le COP d'un CCRS est plus élevé (de façon significative) que celui d'un système frigorifique monoétagé. On peut obtenir une amélioration du COP allant jusqu'à 18,4% pour une température  $T_e$  d'évaporation du RAC/MC de  $-5^\circ\text{C}$ . On a construit puis testé un CCRS prototype lors de l'étude décrite ici. Les résultats expérimentaux montrent qu'à une température  $T_e = -4,5^\circ\text{C}$ , le COP du CCRS est amélioré de 14%. Lorsque  $T_e = 5^\circ\text{C}$ , le COP peut être amélioré de 24% pour un CCRS avec une température de condensation du RAC/MC plus élevée. Cette étude montre qu'un CCRS utilisant un système de refroidissement à éjection en appui du RAC/MC est faisable et rentable. On peut améliorer davantage le COP, puisque ce prototype n'est pas conçu et utilisé dans des conditions optimales. © 2001 Elsevier Science Ltd and IIR. All rights reserved.*

*Mots clés :* Système frigorifique ; Système à compression ; Système à éjection ; Système mixte ; Sous-refroidissement ; Conception ; Performance

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Nomenclature	
$A_e$	effective area of the entrained flow of the ejector ( $m^2$ )
$A_3$	cross-section area of the constant-area section of the ejector ( $m^2$ )
$A_t$	cross-section area of the nozzle throat of the ejector ( $m^2$ )
$COP_1$	coefficient of performance of single-cycle refrigeration system using mechanical compressor (RAC/MC)
$COP_2$	coefficient of performance of combined-cycle refrigeration system using mechanical compressor (RAC/MC) and ejector cooling cycle (EJC)
$d_3$	diameter of the constant-area section in ejector (m)
$d_t$	diameter of the nozzle throat in ejector (m)
$C_p$	specific heat of liquid working fluid in RAC/MC ( $J\ kg^{-1}\ K$ )
$C'_p$	specific heat of liquid working fluid in EJC ( $J\ kg^{-1}\ K$ )
$h$	enthalpy of working fluid ( $J\ kg^{-1}$ )
$h_g$	thermodynamic function of enthalpy for vapor state ( $J\ kg^{-1}$ )
$h_{gs}$	thermodynamic function of enthalpy for saturated-vapor state ( $J\ kg^{-1}$ )
$h_f$	thermodynamic function of enthalpy for saturated-liquid state ( $J\ kg^{-1}$ )
$m_e$	mass flowrate of working fluid in RAC/MC ( $kg\ s^{-1}$ )
$m'_e$	mass flowrate of the ejector suction flow in EJC ( $kg\ s^{-1}$ )
$m'_p$	mass flowrate of the ejector primary flow in EJC ( $kg\ s^{-1}$ )
$P_c$	condensing pressure of RAC/MC (Pa)
$P'_c$	condensing pressure of EJC (Pa)
$P_c^*$	critical condensing pressure of ejector (Pa)
$P_e$	evaporating pressure of RAC/MC (Pa)
	$P'_e$ evaporating pressure of EJC (Pa)
	$P_g$ generating pressure of EJC (Pa)
	$Q_c$ cooling capacity of RAC/MC (W)
	$Q'_c$ cooling capacity of EJC (W)
	$Q_g$ generator heat transfer rate in EJC (W)
	$T$ temperature ( $^{\circ}C$ )
	$T_c$ condensing temperature of the RAC/MC ( $^{\circ}C$ )
	$T'_c$ condensing temperature of the EJC ( $^{\circ}C$ )
	$T_{comp}$ compressor discharge temperature of the RAC/MC ( $^{\circ}C$ )
	$T_e$ evaporating temperature of the RAC/MC ( $^{\circ}C$ )
	$T'_e$ evaporating temperature of the ejector cycle (EJC) ( $^{\circ}C$ )
	$T_g$ generating temperature of the EJC ( $^{\circ}C$ )
	$W_c$ compressor power consumption (W)
	$W_{pump}$ pumping power of pump in ejector-cooling cycle (W)
	$\gamma_p$ compression ratio of the EJC, $P'_c/P'_e$
	$\omega$ ejector entrainment ratio (dimensionless)
	<b>Subscripts</b>
	1,2... thermodynamic state for the process shown in Fig. 1
	c condenser
	e evaporator
	g generator
	NG neck point in generator
	NS neck point in subcooler
	pc precooler
	SC subcooling
	<b>Superscripts</b>
	' ejector-cooling cycle (EJC)
	* critical back pressure condition in ejector

## 1. Introduction

The design and operation of a conventional refrigeration and air-conditioning system using mechanical compressor (RAC/MC) follows the inverse of thermodynamic Rankine cycle. It is well known that subcooling the liquid condensate in a reverse Rankine cycle can increase the COP of a refrigeration system. On the other hand, the compressor outlet temperature in a RAC/MC is high. A plenty amount of high-grade waste energy must be rejected to the environment.

In the present study, we develop a combined-cycle refrigeration system (CCRS) utilizing a heat-driven

ejector-cooling device (EJC) as the bottom cycle of the RAC/MC. The ejector-cooling device is driven thermally by the waste heat of the condenser in the RAC/MC. The cooling capacity obtained from the ejector-cooling device is in turn used to cool the liquid condensate of the RAC/MC to a subcooled state to increase the COP of the RAC/MC (see Fig. 1 for the process). The RAC/MC acts as the top cycle and the EJC acts as the bottom cycle in a CCRS. The heat transfer between these two cycles is linked through an inter-connecting heat transfer unit that is composed of a subcooler for subcooling the refrigerant liquid in the RAC/MC and a generator for vapor generation in the EJC. A precooler

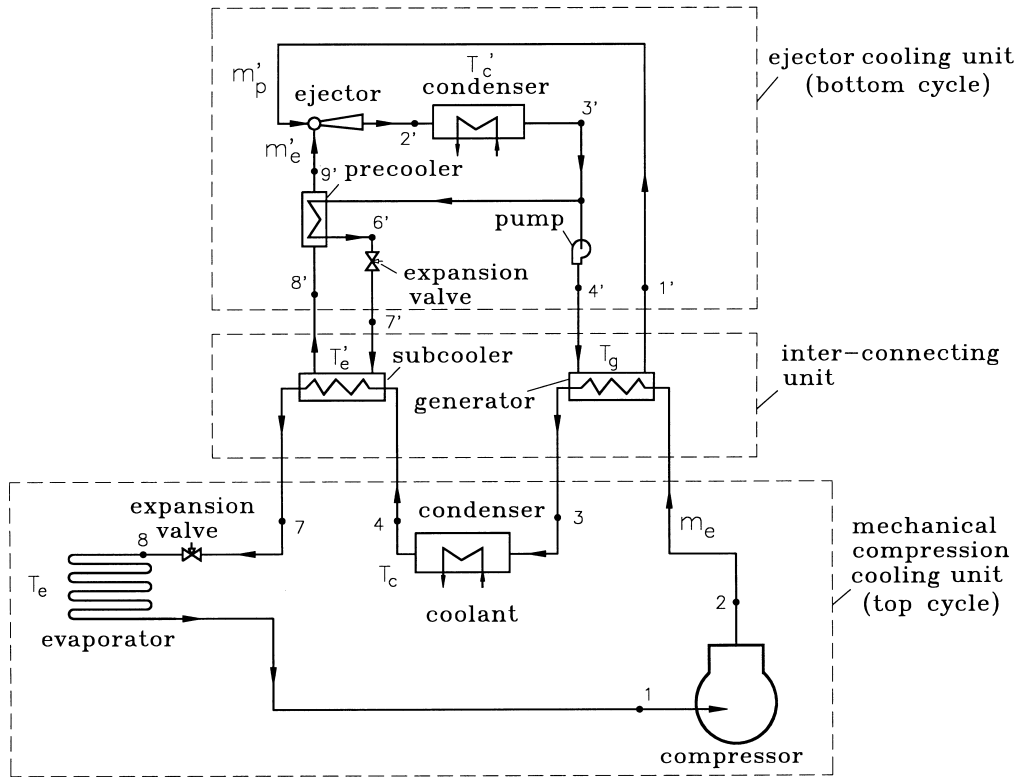


Fig. 1. Schematic diagram of a combined-cycle refrigeration system (CCRS).

Fig. 1. Schéma d'un cycle frigorifique mixte (CCRS).

is used in the EJC to increase the performance of ejector. In this paper, we present the system analysis as well as the test results of a prototype to verify the feasibility of a CCRS.

## 2. System analysis of the combined-cycle refrigeration system

A system analysis of the combined-cycle refrigeration system (CCRS) is carried out in the present study. Governing equations based on the conservation of energy and mass are derived for every component of the CCRS.

### 2.1. Governing equations of the components in CCRS

#### 2.1.1. Subcooler

The subcooler is used to subcool the liquid condensate in the RAC/MC by using the evaporation heat of the EJC. The subcooler is basically a heat exchanger like an evaporator with the refrigerant in the EJC undergoing an evaporating process. We assume that the thermodynamic state at the exit of the subcooler (state

8') for the EJC is a saturated-vapor state and the neck-point (state 7') temperature difference of the subcooler is  $\Delta T_{NS}$ .  $\Delta T_{NS}$  is given as the heat exchanger design parameter. Therefore, we obtain the following governing equations:

$$T'_8 = T'_e = T'_7; \tag{1}$$

$$T_7 = T'_7 + \Delta T_{NS}; \tag{2}$$

$$h'_8 = h_{gs}(T'_8); \tag{3}$$

$$h'_7 = h'_6 \quad (\text{throttling process in expansion valve}); \tag{4}$$

$$Q'_e = m'_e(h'_8 - h'_7) \tag{5}$$

$$Q_e = m_e(h_4 - h_7); \tag{6}$$

$$Q'_e = Q_e = m'_e(h'_8 - h'_7) = m_e(h_4 - h_7). \tag{7}$$

### 2.1.2. EJC condenser

Assume that the condensate at the exit of the condenser (state 3') in the EJC is at saturated-liquid state. The governing equations of the EJC condenser are

$$T'_3 = T'_c \quad (8)$$

$$P'_c = P(T'_c) \quad (9)$$

$$h'_3 = h_{gs}(T'_c) \quad (10)$$

$$h'_2 = h_g(T'_2, P'_c) \quad (11)$$

$$Q'_c = (m'_p + m'_e)(h'_2 - h'_3) \quad (12)$$

### 2.1.3. Generator

In the generator, the refrigerant in the EJC undergoes a phase-change process (evaporation) and the refrigerant in the RAC/MC undergoes a cooling process at vapor state. The generator is thus a heat exchanger like an evaporator. The neck-point temperature difference of the generator is  $\Delta T_{NG}$  which is a given design parameter for the generator. Denoting the state at the neck point as state 02 for the RAC/MC refrigerant vapor and as state 01' for the EJC, we obtain the following governing equations:

$$T_{02} = T_g + \Delta T_{NG} \quad (13)$$

$$m_e(h_{02} - h_3) = m'_e(h'_{01} - h'_4) \quad (14)$$

where  $h_{02} = h_g(T_{02}, P_c)$ ;  $h_2 = h_g(T_2, P_c)$ ;  $h'_{01} = h_f(T'_{01})$ ;

$$T'_{01} = T_g \quad (15)$$

$$T'_4 = T'_3 = T'_c \quad (16)$$

$$h'_4 = h'_{01} - C'_p(T'_{01} - T'_4) = h'_{01} - C'_p(T_g - T'_c) \quad (17)$$

$$m_e(h_2 - h_{02}) = m'_e(h'_1 - h'_{01}) \quad (18)$$

$$\frac{m'_e}{m_e} = \frac{h_2 - h_{02}}{h'_1 - h'_{01}} = \frac{h_{02} - h_3}{h'_{01} - h'_4} \quad (19)$$

$$Q_g = Q'_g = m_e(h_2 - h_3) = m'_e(h'_1 - h'_4). \quad (20)$$

### 2.1.4. RAC/MC condenser

Assuming that the condenser of the RAC/MC has a degree of sub-cooling,  $\Delta T_{SC}$ , the governing equations are

$$Q_c = m_c(h_3 - h_4) \quad (21)$$

$$h_3 = h_g(P_c, T_3) \quad (22)$$

$$T_4 = T_c - \Delta T_{SC}. \quad (23)$$

$$h_4 = h_f(T_c) - C_p \Delta T_{SC} \quad (24)$$

### 2.1.5. EJC precooler

The precooler in the EJC is a simple heat exchanger that can be characterized by the effectiveness:

$$\epsilon_{pc} = \frac{T'_3 - T'_6}{T'_3 - T'_8} \quad (25)$$

$\epsilon_{pc}$  is a given design parameter in the precooler design. Eq. 25 can be used to determine a temperature if the rest two temperatures are known.

### 2.1.6. EJC ejector

The ejector performance can be predicted by a 1-D analysis [1] or by empirical correlations. Huang and Chang [2] experimentally show that the entrainment ratio of the ejector  $\omega$  can be represented by an effective area ratio,  $A_e/A_t$ , and the required ejector area ratio  $A_3/A_t$  is a function of critical condensing pressure  $P'_c$  and the generating pressure  $P_g$ . Here,  $A_e$  represents a hypothetical throat area for the entrained flow of the ejector at choking condition;  $A_t$  is the throat area of the nozzle of the ejector. Empirical correlations for  $A_e/A_t$  and  $A_3/A_t$  were found by Huang and Chang [2] for ejector operated with refrigerant R141b, where  $A_3$  is the cross-section area of the constant-area section of the ejector. Huang and Chang [2] derived the following relations for the calculation of the ejector entrainment ratio:

$$\frac{A_e}{A_t} = -0.0517 \left( \frac{A_3}{A_t} \right)^2 + 1.4362 \left( \frac{A_3}{A_t} \right) - 4.1734 \quad (26)$$

$$\begin{aligned} \frac{A_3}{A_t} &= f_a \left( \frac{P'_c}{P'_c}, \frac{P_g}{P'_c} \right) \\ &= b_0 + b_1 r_c + b_2 r_c^2 + b_3 r_g + b_4 r_c r_g + b_5 r_c^2 r_g \\ &\quad + b_6 r_g^2 + b_7 r_c r_g^2 + b_8 r_c^2 r_g^2 \end{aligned} \quad (27)$$

where  $r_c = P'_c/P'_c$ ;  $r_g = P_g/P'_c$ ;  $b_0 = 5.4497$ ;  $b_1 = -6.7759$ ;  $b_2 = 1.4952$ ;  $b_3 = 2.3116$ ;  $b_4 = -0.590$ ;  $b_5 = 0.018105$ ;  $b_6 = -0.03786$ ;  $b_7 = 0.012983$ ;  $b_8 = -0.000812145$ . Assuming that  $P'_c = P'_c$ , and using the above correlations and the calculation procedure derived by Huang and Chang [2], the entrainment ratio of the ejector can be determined.

From energy balance, the following governing equations are also obtained:

$$h'_2 = \frac{h'_1 + \omega h'_0}{1 + \omega} \quad (28)$$

$$T'_2 = h_g(P'_c, h'_2) \tag{29}$$

where  $\omega = m'_c/m'_p$ .

2.1.7. RAC/MC compressor

The compressor undergoes a non-isentropic process for vapor compression. The power input to the compressor can be represented by the following equation:

$$W_c = m_c(h_2 - h_1)/\eta_c \tag{30}$$

where  $\eta_c$  is the compression efficiency, including the motor loss. The outlet temperature  $T_2$  of the compressor can be determined by thermodynamic equation of state:

$$T_2 = f(h_2, P_c) \tag{31}$$

where

$$h_2 = h_1 + (h_{2s} - h_1)/\eta_s \tag{32}$$

$$h_{2s} = h_g(T_{2s}, P_c) \tag{33}$$

$$T_{2s} = h_g(P_c, s_2 = s_1) \tag{34}$$

$\eta_s$  is the isentropic efficiency of the compression process.

2.2. System analysis of a CCRS

Using the above governing equations, a system performance calculation based on the concept of information-flow diagram [3] can be carried out. The information-flow diagram shows that there are three independent design variables for a CCRS, namely, the condensing temperature  $T_c$  and the evaporating temperature  $T_e$  of the RAC/MC, and the evaporating temperature  $T'_e$  of the EJC. Given  $T_c$ ,  $T_e$ ,  $T'_e$  and the performance maps of the

ejector and the compressor, the system performance of a CCRS can be carried out.

In the present study, we use R22 as the working fluid in the RAC/MC and R141b as the working fluid in the EJC. Eqs. (26) and (27) are used for ejector performance calculation in system analysis since R141b is used in EJC. The RAC/MC uses a reciprocating-type compressor S34UP which is made by Electrolux. The rated power is 1-7/8 HP and the swept volume of the piston is 34 cm<sup>3</sup>. The compressor efficiency  $\eta_c$  was separately determined by an experiment and the following empirical relation is obtained:

$$\eta_c = 0.9172 - 0.1031(P_c/P_e) \tag{35}$$

The coefficient of performance of the combined-cycle refrigeration system,  $COP_2$ , is determined by the following definition:

$$COP_2 = \frac{Q_c}{W_c + W_{pump}}, \tag{36}$$

where  $W_{pump}$  is the pumping power consumed by the circulation pump in the EJC. For comparison, the coefficient of performance of the single-cycle refrigeration system (RAC/MC),  $COP_1$ , is determined.  $COP_1$  is defined as

$$COP_1 = \frac{Q_c}{W_c}. \tag{37}$$

The analytical results presented in Table 1 show that the COP of a CCRS is superior to that of a single-cycle system (RAC/MC). It can be seen that the improvement of COP is more significant at higher condensing temperature of the RAC/MC  $T_c$ . For  $T_e = -5^\circ\text{C}$ , the improvement in COP by using a CCRS can be as high as 18.4% at  $T_c = 50^\circ\text{C}$  and  $T'_e = 20^\circ\text{C}$  (evaporating temperature of the EJC). Fig. 2 shows that the ejector

Table 1 Analytical results for COP of single-cycle and combined-cycle systems at  $T_e = -5^\circ\text{C}$

Tableau 1 COP de systèmes simples et mixtes à une température  $T_e$  de  $-5^\circ\text{C}$  : résultats de l'analyse

R22 condensing temperature $T_c$ ( $^\circ\text{C}$ )	Single-cycle system $COP_1$	$T'_e = 20^\circ\text{C}$		$T'_e = 22^\circ\text{C}$		$T'_e = 24^\circ\text{C}$	
		$COP_2$	$\Delta COP_{imp}^a$ (%)	$COP_2$	$\Delta COP_{imp}^a$ (%)	$COP_2$	$\Delta COP_{imp}^a$ (%)
35	2.33	2.50	7.3	2.48	6.2	2.45	5.2
38	2.11	2.31	9.5	2.29	8.1	2.26	7.0
40	1.98	2.20	11.1	2.17	9.5	2.15	8.6
42	1.83	2.05	12.0	2.03	10.9	2.01	9.8
45	1.64	1.88	14.6	1.86	13.3	1.84	12.2
47	1.53	1.77	15.7	1.75	14.8	1.73	13.1
50	1.36	1.61	18.4	1.59	17.2	1.57	15.4

<sup>a</sup>  $\Delta COP_{imp} = (COP_2 - COP_1)/COP_1 \times 100\%$ .

entrainment ratio  $\omega$  increases with increasing  $T_c$  and  $T'_e$ . The required ejector area ratio  $A_3/A_t$  increases with increasing  $T_c$  and decreasing  $T'_e$  as shown in Figs. 3. Figs. 4 and 5 show that the cooling capacity  $Q_e$  and the COP of a CCRS is superior to that of a single-cycle system. The higher the condensing temperature  $T_c$ , the better the improvement in COP by using a CCRS. This indicates that a CCRS may be more significant for an ice-storage air-conditioning system using a condenser with air cooling device.

### 3. Prototype design and test of a combined-cycle refrigeration system

#### 3.1. Prototype design

A prototype was designed based on the previous system analysis. The design point of the prototype is selected for ice-storage air-conditioning application with

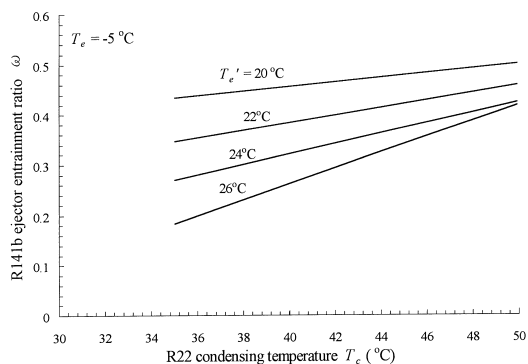


Fig. 2. Theoretical prediction of ejector entrainment ratio  $\omega$  in CCRS.

Fig. 2. Taux d'entraînement  $\omega$  du CCRS : prévision théorique.

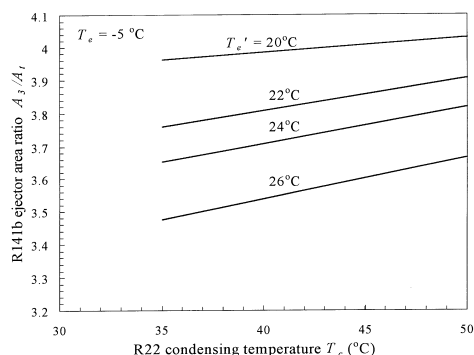


Fig. 3. Theoretical prediction of ejector area ratio  $A_3/A_t$  in CCRS.

Fig. 3. Prévision théorique de du rapport des sections caractéristiques de l'éjecteur  $A_3/A_t$  du CCRS.

$T_e = -5^\circ\text{C}$ ,  $T_c = 38^\circ\text{C}$ ,  $T'_e = 20^\circ\text{C}$ ,  $T_c = 32.5^\circ\text{C}$  and  $T_g = 68^\circ\text{C}$ . The design-point specification of the prototype is summarized in Table 2.

#### 3.2. Prototype test

The facilities used to measure the cooling capacity  $Q_e$  of the prototype, the flowrate of R141b, the temperature and pressure of the cycle at various position, etc., are all the same as described in the previous paper [2].

First of all, we compare the test results of the CCSR with the system analysis at experimental values of  $T'_e$  and  $T_c$ , including off-design conditions. Table 3 shows that the analytical results are slightly higher than the test results, within 20% error for  $\text{COP}_2$  at  $T_e = +5^\circ\text{C}$  and within 13% for  $\text{COP}_2$  at  $T_e = -5^\circ\text{C}$ . This is due to the heat loss in the pipelines and the heat exchangers

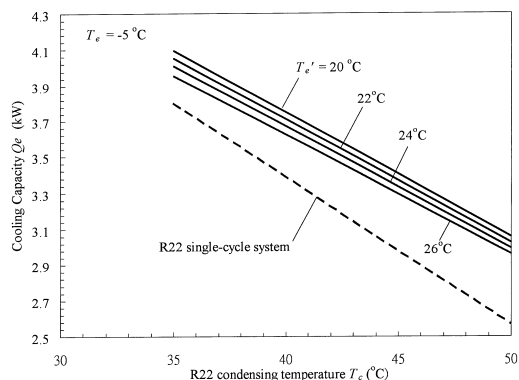


Fig. 4. Theoretical prediction of cooling capacity  $Q_e$  for CCRS and RAC/MC.

Fig. 4. Prévision théorique de la puissance frigorifique  $Q_e$  pour le CCRS et le RAC/MC.

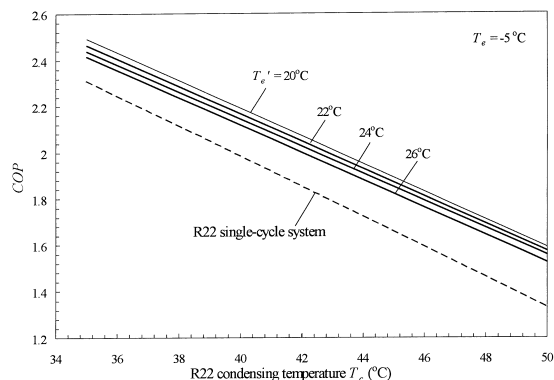


Fig. 5. Theoretical prediction of cooling capacity COP for CCRS and RAC/MC.

Fig. 5. Prévision théorique du COP, en termes de puissance frigorifique, pour le CCRS et le RAC/MC.

that are not well insulated. The pressure loss in pipelines and heat exchanger is also a factor causing the analytical error.

Table 4 presents the test results of single-cycle and combined-cycle refrigeration systems at  $T_e = -4.5^\circ\text{C}$ . The operating conditions in the tests include the off-design conditions. It is seen from Table 4 that the improvement in COP of the CCRS is in the range 9–14%. The entrainment ratio  $\omega$  of the R141b ejector varies from 0.5 to 0.77 and the COP of the EJC is 0.43–0.67 for compression ratio  $\gamma_p$  of the ejector from 1.22 to 1.67.

Table 2  
Design specifications of the prototype

Tableau 2  
Spécifications du prototype

1. R22 compressor cycle (RAC/MC)	
Compressor	Electrolux S34UP (1-7/8 HP), 34 cm <sup>3</sup>
Evaporator	5.2 kW flat-plate type
Condenser	7.1 kW flat-plate type, water cooling
Expansion device	1.4 mm ID capillary tube, 80 cm
2. R141b ejector cooling cycle (EJC)	
Ejector	$d_t = 1.6$ mm; $d_3 = 4.0$ mm
Evaporator	1.9 kW flat-plate type
Condenser	4.6 kW flat-plate type, water cooling
Precooler	4.6 kW flat-plate type
Expansion device	3/8" adjustable expansion valve
R141b pump	5 l/min, gear pump
3. Design-point performance of combined-cycle system	
Cooling capacity $Q_c$	3.9 kW
COP <sub>2</sub>	2.31

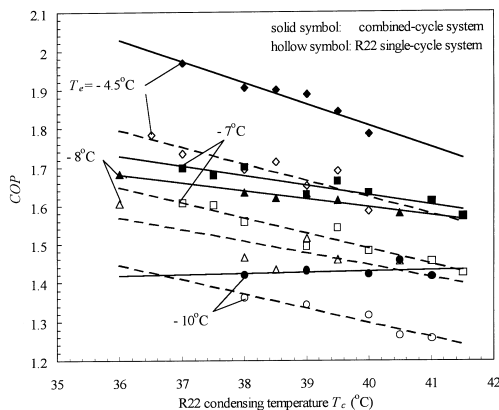


Fig. 6. Experimental results of a combined-cycle refrigeration system for  $T_e$  from  $-10$  to  $-4.5^\circ\text{C}$ .

Fig. 6. Résultats expérimentaux d'un système frigorifique mixte pour les  $T_e$  allant de  $-10$  à  $-4,5^\circ\text{C}$ .

The off-design test is also performed at  $T_e = 5^\circ\text{C}$ . Table 5 shows that the COP improvement of the CCRS is in the range of 15–24%. The entrainment ratio  $\omega$  of the R141b ejector is from 0.51 to 0.90 and the COP of the EJC is 0.46–0.80 for ejector compression ratio  $\gamma_p$  from 1.12 to 1.19. It is seen that the performance improvement of a CCRS has the highest value at high  $T_c$ . This coincides with the theoretical prediction and indicates that the CCRS may be more significant if used in an air-conditioning system with air-cooled condenser.

Test results for various off-design conditions are shown in Figs. 6 and 7 for various  $T_e$  and  $T_c$ . From these results, we may conclude that the CCRS can significantly improve the performance of a single-cycle refrigeration system (RAC/MC).

4. Discussion and conclusion

The use of the ejector cooling cycle (EJC) as the bottom cycle of an inverse Rankine cycle using mechanical compressor (RAC/MC) to lead to a combined-cycle refrigeration system (CCRS) is a new concept. Since the ejector-cooling cycle is driven using the waste heat from the RAC/MC, no additional energy is required except the negligible pumping power in the EJC. The improvement in COP for a CCRS is thus expected. Both the system simulation and the experimental results obtained in the present study verify this concept. The improvement of COP for the present laboratory-made prototype with small capacity and tested at off-design conditions can be as large as 24%, and are mostly greater than 10% depending upon the operating conditions. Further improvement in COP is possible since the prototype is

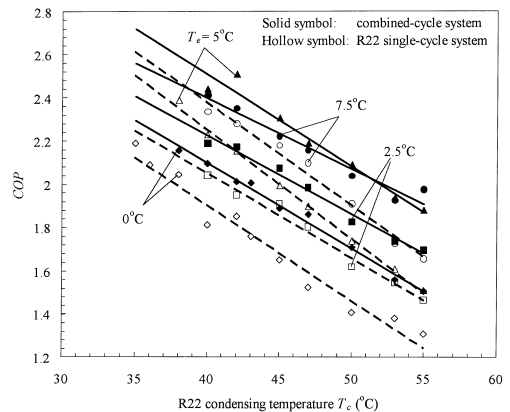


Fig. 7. Experimental results of a combined-cycle refrigeration system for  $T_e$  from 0 to  $7.5^\circ\text{C}$ .

Fig. 7. Résultats expérimentaux d'un système frigorifique mixte pour les  $T_e$  allant de 0 à  $+7,5^\circ\text{C}$ .

Table 3  
Comparison of analytical and test results for a combined-cycle refrigeration system at  $T_e = -5$  and  $+5^\circ\text{C}$

Tableau 3  
Comparaison des résultats analytiques et d'essais pour un système frigorifique mixte pour  $T_e = -5$  et  $+5^\circ\text{C}$

R22 condensing temperature $T_c$ ( $^\circ\text{C}$ )	Cooling capacity $Q_e$ (kW)			Compressor input power $W_c$ (kW)			$COP_2$		
	Analysis	Test	Error <sup>a</sup> (%)	Analysis	Test	Error <sup>a</sup> (%)	Analysis	Test	Error <sup>a</sup> (%)
$T_e = -5^\circ\text{C}$									
38 ( $T'_c = 16^\circ\text{C}$ )	3.97	3.09	+22.2	1.68	1.59	+5.4	2.36	1.90	+19.5
40 ( $T'_c = 21^\circ\text{C}$ )	3.76	2.97	+21.0	1.72	1.63	+5.2	2.18	1.79	+12.2
$T_e = +5^\circ\text{C}$									
42 ( $T'_c = 27^\circ\text{C}$ )	5.65	4.83	+14.5	1.98	1.87	+5.6	2.86	2.51	+12.2
45 ( $T'_c = 27^\circ\text{C}$ )	5.45	4.62	+15.2	2.08	1.94	+6.7	2.62	2.31	+11.8
50 ( $T'_c = 27^\circ\text{C}$ )	5.20	4.46	+14.2	2.26	2.06	+8.8	2.32	2.29	+1.30

<sup>a</sup> Error =  $(COP_{\text{analysis}} - COP_{\text{test}}) / COP_{\text{analysis}} \times 100\%$ .

Table 4  
Comparison of test results for single-cycle and combined-cycle refrigeration systems at  $T_e = -4.5^\circ\text{C}$

Tableau 4  
Comparaison des résultats d'essais sur des systèmes simples et mixtes où  $T_e = -4.5^\circ\text{C}$

R22 $T_c$ ( $^\circ\text{C}$ )	R22 single-cycle system				Combined-cycle system		
	$Q_e$ (kW)	$T_{\text{comp}}$ ( $^\circ\text{C}$ )	$m_e$ (kg/s)	$COP_1$	$Q_e$ (kW)	$COP_2$	$\Delta COP_{\text{imp}}$ (%)
37	2.718	104.8	0.0155	1.735	3.131	1.969	13.53
38	2.693	109.2	0.0157	1.694	3.091	1.904	12.44
38.5	2.741	106.1	0.0156	1.714	3.071	1.898	10.76
39	2.652	103.8	0.0155	1.651	3.103	1.887	14.27
39.5	2.726	106.6	0.0163	1.690	3.026	1.843	9.03
40	2.590	107.2	0.0150	1.586	2.966	1.785	12.56

Performance of R141b ejector-cooling unit at  $T_e = -4.5^\circ\text{C}$

R22 $T_c$ ( $^\circ\text{C}$ )	$T_g$ ( $^\circ\text{C}$ ) (kPa)	$T'_c$ ( $^\circ\text{C}$ ) (kPa)	$T''_c$ ( $^\circ\text{C}$ ) (kPa)	$\gamma_p$	$Q'_e$ (kW)	$Q'_g$ (kW)	$\omega$	$COP_{\text{R141b}}$
37	70.8 (330)	18.5 (60.5)	26 (80)	1.33	0.329	0.493	0.766	0.667
38	71.6 (340)	16.0 (53.9)	29 (90)	1.67	0.316	0.562	0.654	0.563
38.5	70.3 (330)	16.0 (53.9)	29 (90)	1.67	0.290	0.534	0.629	0.544
39	69.5 (320)	18.5 (60.5)	29 (90)	1.49	0.305	0.508	0.688	0.600
39.5	71.5 (340)	21.0 (67.1)	32 (100)	1.49	0.256	0.556	0.531	0.462
40	72.3 (350)	21.0 (67.1)	32 (100)	1.49	0.216	0.497	0.501	0.434



Table 5

Comparison of test results for single-cycle and combined-cycle refrigeration systems at  $T_e = +5^\circ\text{C}$

Tableau 5

Comparaison des résultats d'essais sur des systèmes simples et mixtes où  $T_e = +5^\circ\text{C}$

R22 $T_c$ ( $^\circ\text{C}$ )	R22 single-cycle system				Combined-cycle system		
	$Q_e$ (kW)	$T_{\text{comp}}$ ( $^\circ\text{C}$ )	$m_e$ (kg/s)	$COP_1$	$Q_e$ (kW)	$COP_2$	$\Delta COP_{\text{imp}}$ (%)
42	4.01	106.4	0.0259	2.15	4.83	2.5072	16.61
45	3.91	111.8	0.0238	1.99	4.62	2.3077	15.96
47	3.80	112.3	0.0235	1.90	4.53	2.1892	15.22
50	3.60	114.7	0.0244	1.74	4.46	2.0893	20.07
53	3.44	120.6	0.0240	1.61	4.30	1.9371	20.32
55	3.28	123.3	0.0238	1.51	4.23	1.8793	24.46

Performance of R141b ejector-cooling unit at $T_e = 5^\circ\text{C}$								
R22 $T_c$ ( $^\circ\text{C}$ )	$T_g$ ( $^\circ\text{C}$ ) (kPa)	$T'_e$ ( $^\circ\text{C}$ ) (kPa)	$T'_c$ ( $^\circ\text{C}$ ) (kPa)	$\gamma_p$	$Q'_e$ (kW)	$Q'_g$ (kW)	$\omega$	$COP_{\text{R141b}}$
42	70.2 (300)	25.5 (80.3)	31 (94.7)	1.179	0.297	0.667	0.508	0.446
45	70.4 (310)	27.0 (84.2)	32 (100)	1.188	0.299	0.640	0.527	0.467
47	70.9 (300)	27.5 (86.8)	31 (97.4)	1.122	0.366	0.626	0.668	0.585
50	70.3 (300)	27.5 (86.8)	31 (97.4)	1.122	0.458	0.644	0.805	0.710
53	72.1 (300)	27.5 (86.8)	31 (97.4)	1.122	0.500	0.658	0.854	0.670
55	73.0 (300)	27.5 (86.8)	31 (97.4)	1.122	0.545	0.679	0.897	0.802

not designed and tested at an optimal condition. Further experiments using full-scale system ( $Q_e > 5\text{RT}$ ) is also needed before field application. It is expected that the performance improvement of a CCRS may even be higher than the present results.

Finally, it is also noted that the feasibility of the CCRS depends on the reliability that is related to the discharge temperature of the compressor. The test results presented in Tables 4 and 5 show that the discharge temperatures  $T_{\text{comp}}$  of the compressor are all maintained in a safe region ( $< 125^\circ\text{C}$ ). Actually, for all the test runs, the compressor has never been shut down automatically by the thermal protection device attached to the compressor body. In practice, the compressor discharge temperature will not exceed the limit if the CCRS is carefully designed. This can be achieved by using a good ejector with optimal design and good fabrication technique, a good condensing device of the EJC, good refrigerant for the EJC, the good matching expansion device in the RAC/MC, or the optimal amount of refrigerant charge in the RAC/MC. A series of test runs for a new prototype built recently reveal that the discharge temperature of the compressor is maintained between  $100^\circ\text{C}$  and  $115^\circ\text{C}$  for the similar

operating conditions shown in Tables 4 and 5. This assures that a CCRS can be designed to meet the practical requirement on the reliability issue, in addition to increasing the COP.

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